

**Coherent Pion Production  
in the Neutrino-Nucleus Scattering  
in Few-GeV Region**

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# Introduction

## New neutrino oscillation experiments

(T2K, MiniBooNE, ...)

- \* Neutrino in few GeV region
- \* Detection through neutrino-nucleus scattering
- \* Need reliable model for neutrino-nucleus scattering

# Neutrino-nucleus scattering in few GeV region

## sub-dominant

- \* Coherent  $\pi$  production :  $\nu A \rightarrow \mu^- \pi^+ A$ 
  - Hadronic model : Rein and Sehgal, PLB **223**, 29 (1983)  
Singh *et al.*, PRL **96**, 241801 (2006)  
Alvarez-Ruso *et al.*, PRC **75**, 055501 (2007)
  - PCAC : Kartavtsev *et al.*, PRD **74**, 054007 (2006)  
Rein and Sehgal, PLB **657**, 207 (2007)

## dominant

- \* Quasi-elastic :  $\nu A \rightarrow \mu^- N(A - 1)$
- \* 1  $\pi$  production (Quasi-free) :  $\nu A \rightarrow \mu^- \Delta(A - 1)$   
 $\rightarrow \mu^- \pi N(A - 1)$

## Model

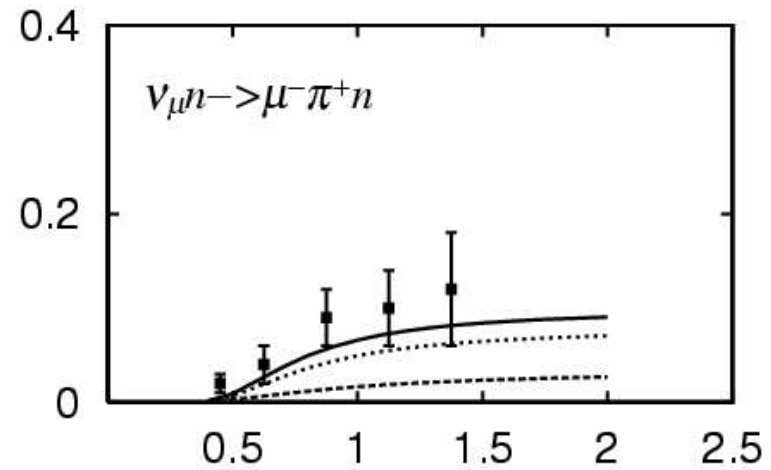
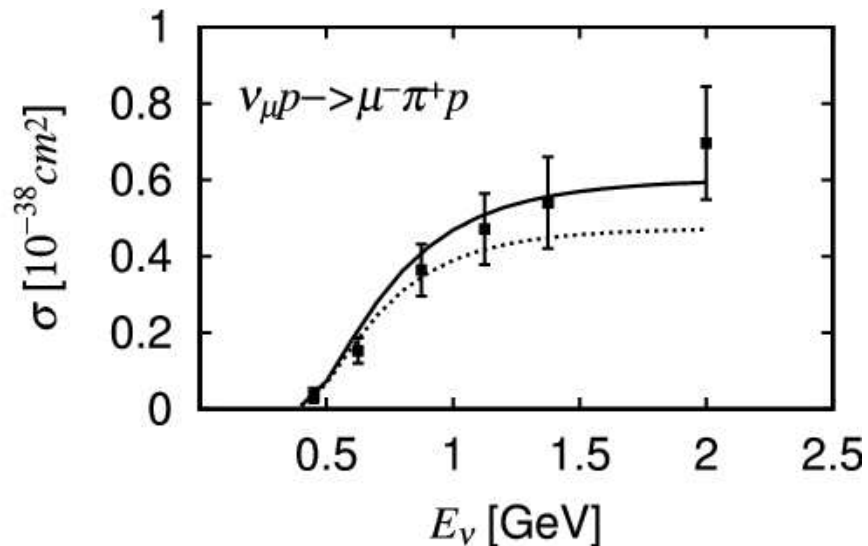
- \* Elementary process amplitudes ( $\nu N \rightarrow \mu^- \pi^+ N$ )  
→ **SL** (Sato-Lee) **model** [PRC **54**, 2660 (1996); **67**, 065201 (2003)]
- \* Medium effect on  $\Delta$  (mass and width)  
Final state interaction ( $\pi$ -nucleus optical potential)  
→  **$\Delta$ -hole model** [*e.g.*, Koch and Moniz, PRC **27**, 751 (1983)]
- \* Nuclear form factor  
→ empirical form factor (electron scattering)

*Combine SL and  $\Delta$ -hole model !*

## SL model

[Sato and Lee, PRC **54**, 2660 (1996); **67**, 065201 (2003)]

- \* Model for electroweak  $\pi$  production off nucleon in  $\Delta$  region
- \* Non-perturbative amplitudes ( $\pi$  cloud)
- \* Large amount of data (JLab, BNL) for  $(\gamma, \pi^0)$  and  $(e, e'\pi^0)$  are consistently described



# Optical potential for $\pi$ -nucleus scattering

[Karaoglu *et al.*, PRC **33**, 974 (1986)]

$$U_{\pi A} \sim F(\vec{q}) \tilde{t}_{\pi N} + W \rho^2$$

$F(\vec{q})$  : nuclear form factor for  $\vec{q}$  (momentum transfer)

$t_{\pi N}$  :  $\pi N$  scattering amplitude (SL model)  $\rightarrow \tilde{t}_{\pi N}$

$$\frac{1}{E - m_{\Delta} - i\Gamma/2} \rightarrow \frac{1}{E - m_{\Delta} - i\Gamma/2 - H_{\Delta} - \Sigma_{Pauli} - \Sigma_{spr}}$$

$$\Sigma_{spr} = V_C \rho(r) + V_{LS}(r) \vec{L} \cdot \vec{S}$$

$W$  : phenomenological term (two-body  $\pi$  absorption)

Parameters (complex) :  $V_C, V_{LS}, W_s, W_p \rightarrow \pi$ -nucleus scattering data

Transition amplitude for  $\lambda A \rightarrow \pi A$  ( $\lambda$  : external probe)

$$A_{\lambda A \rightarrow \pi A} \sim \int d\vec{p}_\pi \psi_{\pi A} F(\vec{q}) \tilde{A}_{\lambda N \rightarrow \pi N}$$

$\psi_{\pi A}$  :  $\pi$  wave function (final state interaction,  $U_{\pi A}$ )

$A_{\lambda N \rightarrow \pi N}$  :  $\lambda N \rightarrow \pi N$  amplitude (SL model)  $\rightarrow \tilde{A}_{\lambda N \rightarrow \pi N}$

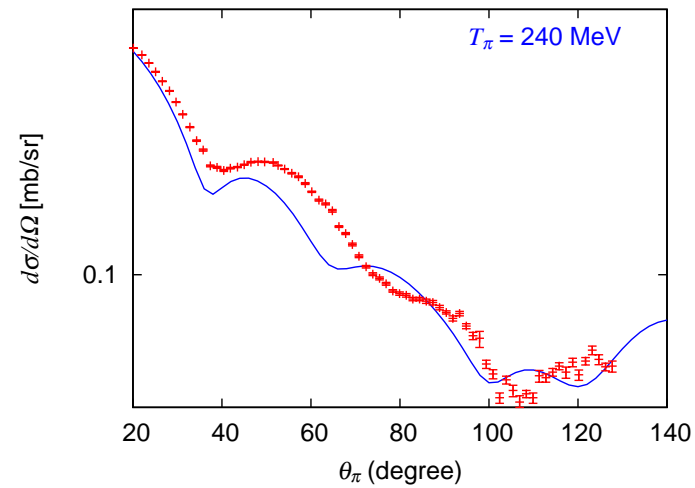
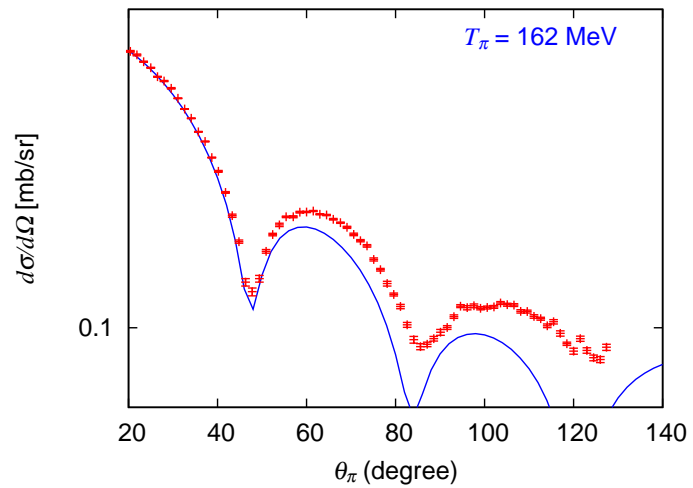
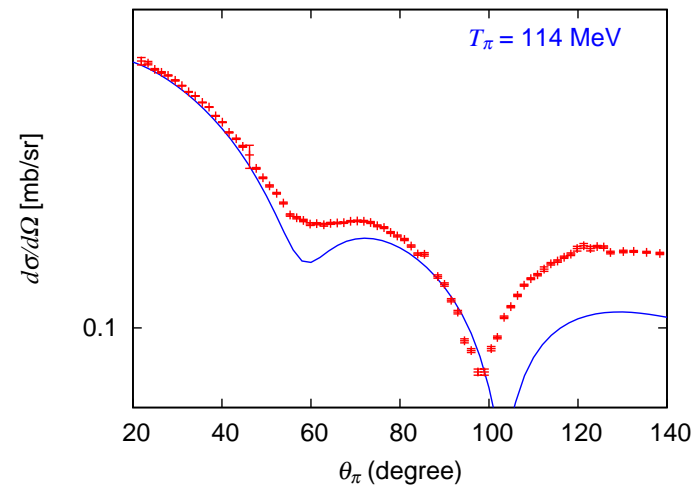
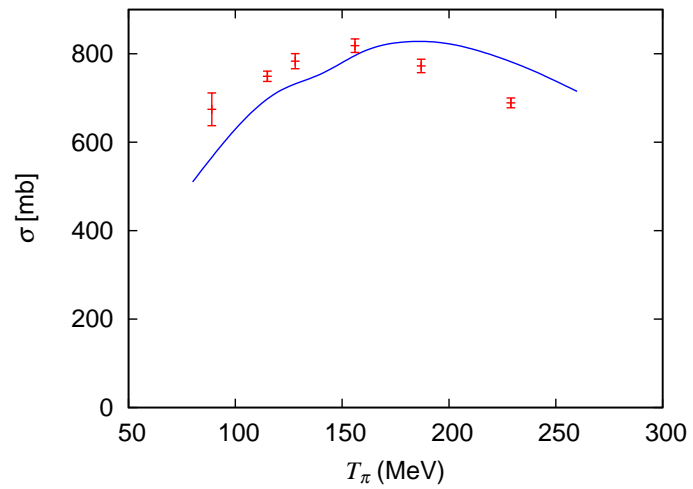
$$\frac{1}{E - m_\Delta - i\Gamma/2} \rightarrow \frac{1}{E - m_\Delta - i\Gamma/2 - H_\Delta - \Sigma_{Pauli} - \Sigma_{spr}}$$

All parameters fixed by  $\pi$ -nucleus data

$\rightarrow$  parameter-free prediction for  $\lambda A \rightarrow \pi A$

# Results

## I. $\pi^+$ - $^{16}\text{O}$ scattering (Parameters fitted to data)

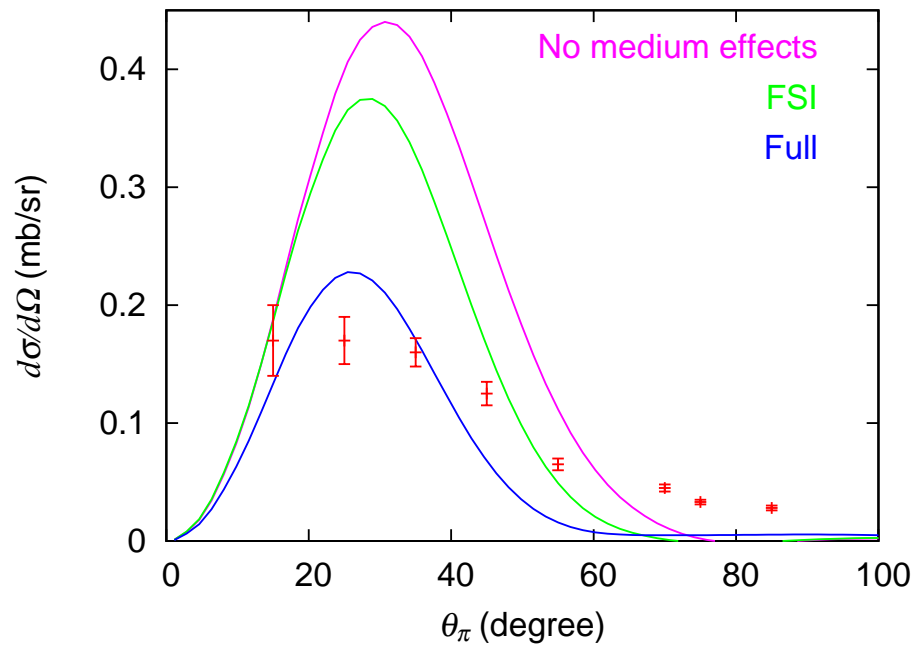


[Data: NPB **76**, 15 (1974); NPA **350**, 301 (1980)]



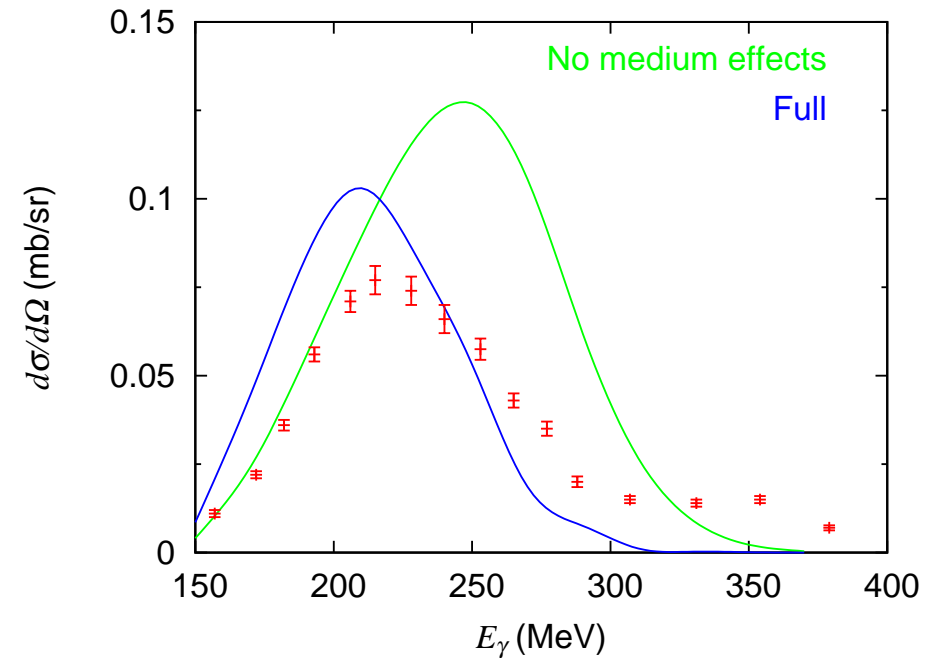
## II. Photo coherent $\pi$ production $(\gamma + {}^{12}\text{C} \rightarrow \pi^0 + {}^{12}\text{C}_{g.s.})$

$E_\gamma = 290 \text{ MeV}$



[Data: Z. Phys.A **311**, 367 (1983)]

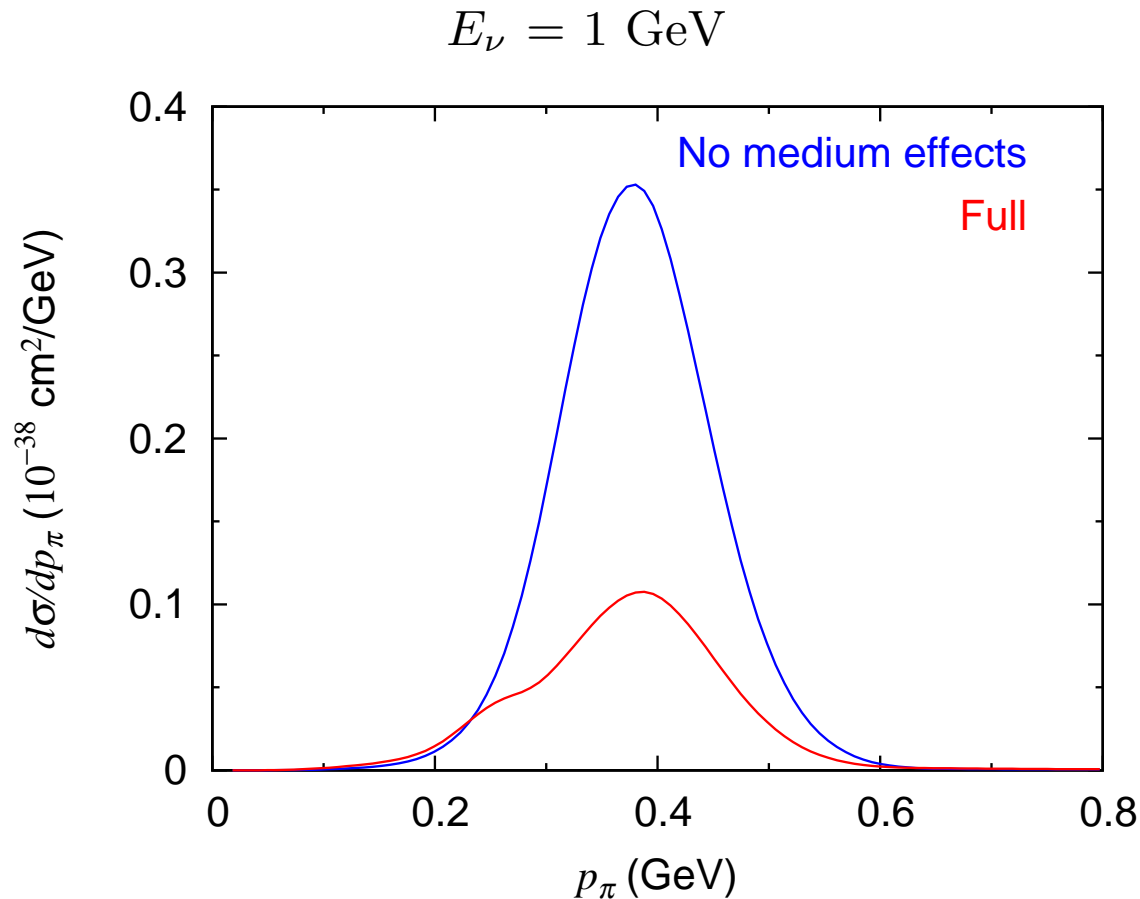
$\theta_\pi = 60^\circ$



[Data: Schmitz (A2 collaboration),  
PhD thesis (1996)]

- Parameter-free prediction
- Important medium effects

### III. Neutrino coherent $\pi$ production $(\nu_\mu + {}^{12}\text{C} \rightarrow \mu^- + \pi^+ + {}^{12}\text{C}_{g.s.})$



$$\sigma_{\text{total}} = 2.1 \times 10^{-40} \text{ cm}^2$$

$(E_\nu = 1 \text{ GeV})$

$$\sigma_{\text{EXP}} < 7.7 \times 10^{-40} \text{ cm}^2$$

(spectrum averaged)

[Data: Hasegawa *et al.* (K2K),  
PRL **95**, 252301 (2005)]

Consistent with data

Different from other calculations (under investigation)

## Summary

Development of theoretical model for new neutrino experiments !

*SL model +  $\Delta$ -hole model* for unified description of:

- $\pi$ -nucleus scattering
- photo coherent  $\pi$  production
- neutrino coherent  $\pi$  production

Overall, data are reproduced fairly well  
*particularly, consistent with data from K2K !*

# Future plan

## Short term

Further study on neutrino coherent  $\pi$  production

- Some refinements (parameters ...etc.)
- NC process (MiniBooNE data)
- Anti-neutrino process

## After that

Single  $\pi$  production (quasi-free process)