

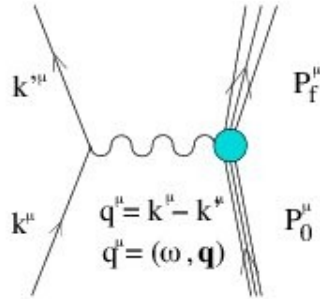
Electron scattering off ^4He with Three-Nucleon forces

in collaboration with S. Bacca (TRIUMF), N. Barnea (Hebrew University),
G. Orlandini (Univ. of Trento)

Outline:

- Brief summary of formalism for inclusive electron scattering
- Ingredients/methods of the performed *ab initio* calculation with realistic nuclear forces
- Results

Ab initio electron scattering



Inclusive process $A(e, e')X$

$$\frac{d^2\sigma}{d\Omega d\omega} = \sigma_M \left[\frac{Q^4}{\mathbf{q}^4} R_L(\omega, \mathbf{q}) + \left(\frac{Q^2}{2\mathbf{q}^2} + \tan^2 \frac{\theta}{2} \right) R_T(\omega, \mathbf{q}) \right]$$

$$R_L(\omega, \mathbf{q}) = \sum_f |\langle \Psi_f | \rho(\mathbf{q}) | \Psi_0 \rangle|^2 \delta \left(E_f - E_0 - \omega + \frac{\mathbf{q}^2}{2M} \right)$$

$$\rho(\mathbf{q}) = \sum_{NR} e^{i\mathbf{q} \cdot \mathbf{r}'_k} \frac{1 + \tau_k^3}{2}$$

Purpose \longrightarrow Investigate the effect of **three-nucleon forces** on $R_L(\omega, \mathbf{q})$

Nuclear forces employed: NN \longrightarrow AV18
 NNN \longrightarrow UIX

Results with

LIT + EIH

The Lorentz Integral Transform (LIT)

Efros, Leidemann, Orlandini, PLB 338 (1994) 13

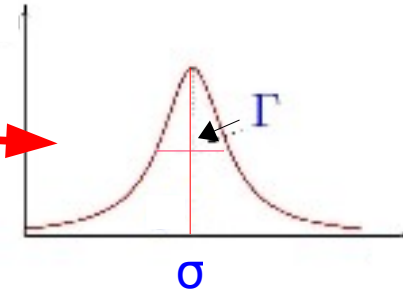


$$R(\omega) = \sum_f \left| \langle \psi_f | \hat{O} | \psi_0 \rangle \right|^2 \delta(E_f - E_0 - \omega)$$



$$L(\sigma, \Gamma) = \int d\omega \frac{R(\omega)}{(\omega - \sigma)^2 + \Gamma^2} = \langle \tilde{\psi} | \tilde{\psi} \rangle$$

$$(H - E_0 - \sigma + i\Gamma) | \tilde{\psi} \rangle = \hat{O} | \psi_0 \rangle$$



Calculation of ground state and of LIT $L(\sigma, \Gamma)$ via expansions in Hyperspherical Harmonics (HH).

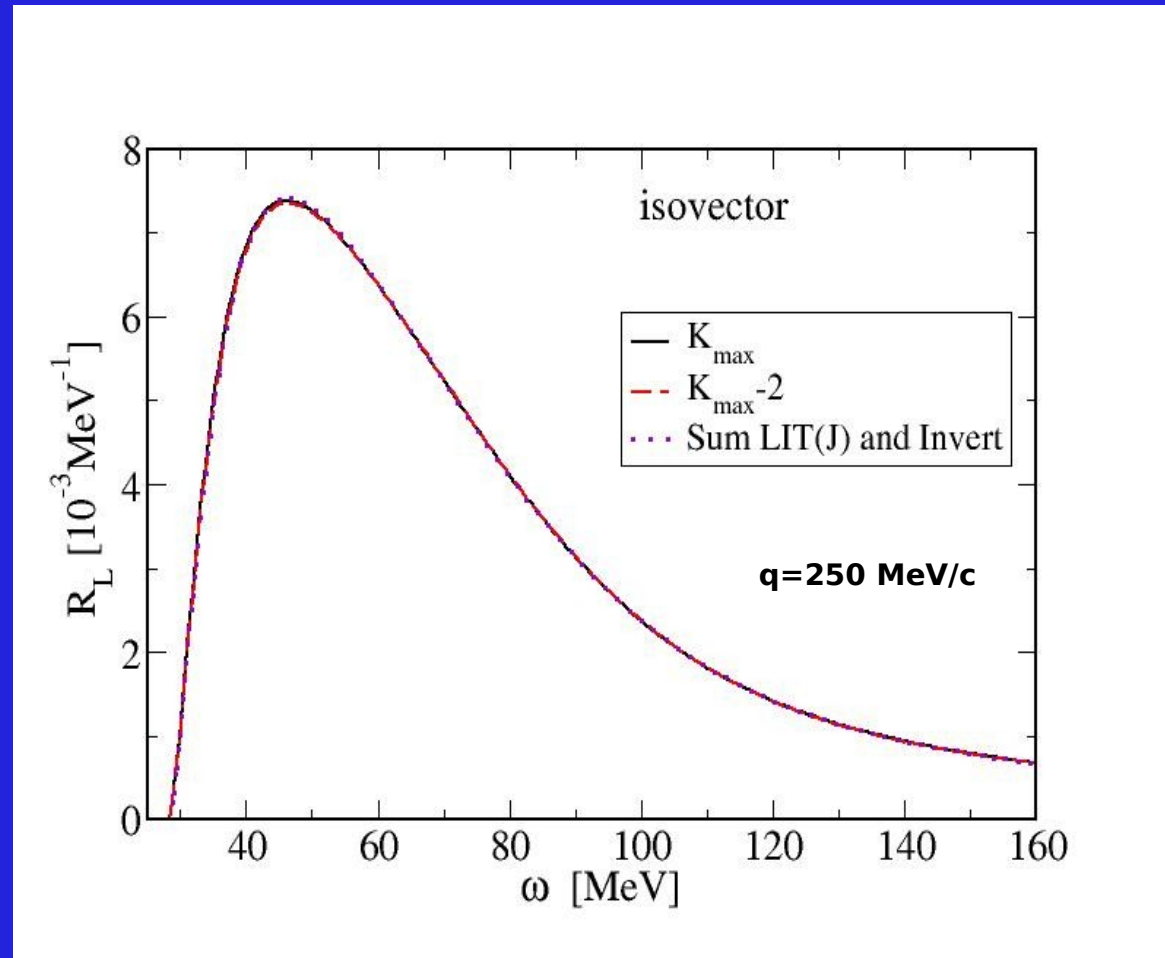
HH expansions have a very slow convergence rate for nuclear physics problems. Strong acceleration of convergence is obtained by the so-called Effective Interaction HH (EIHH).

EIHH: unitary transformation of bare interaction in a given model space leads to an effective interaction for model space; steady increase of model space up to the point that convergent ground-state/LIT results are obtained (similar to NCSM).

Barnea, W.L., Orlandini, PRC 61, 054001 (2000)

Precision of obtained results

- Convergence check of HH expansion
- Check of inversion

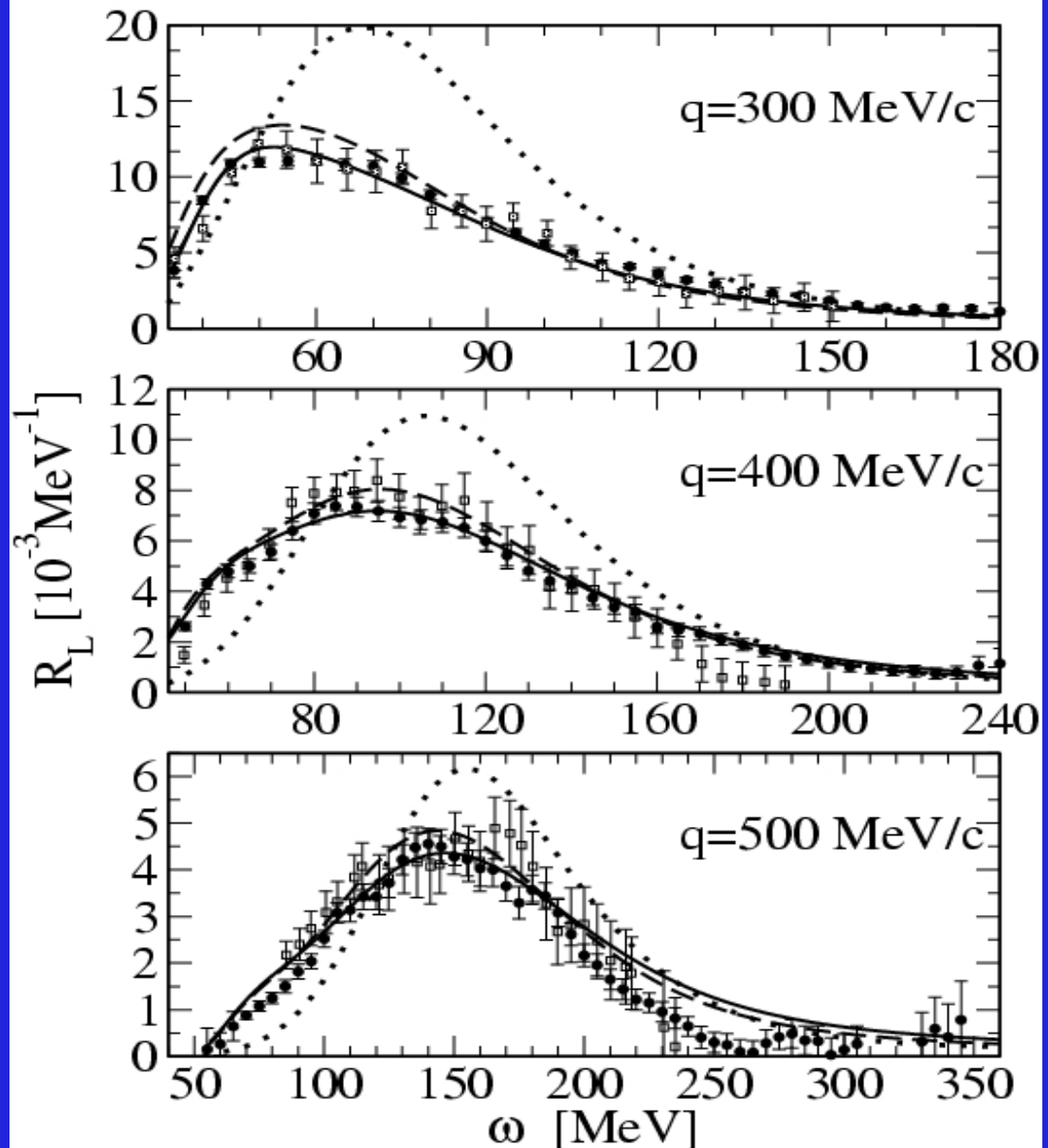


$R_L(\omega, q)$ of ${}^4\text{He}$



- ★ Large FSI effects
- ★ 10% reduction due to 3BF
- ★ rather good agreement with data

At $q=500$ MeV/c relativistic effects could become more important (see my poster on $R_{L/T}(\omega, q)$ of ${}^3\text{He}$)

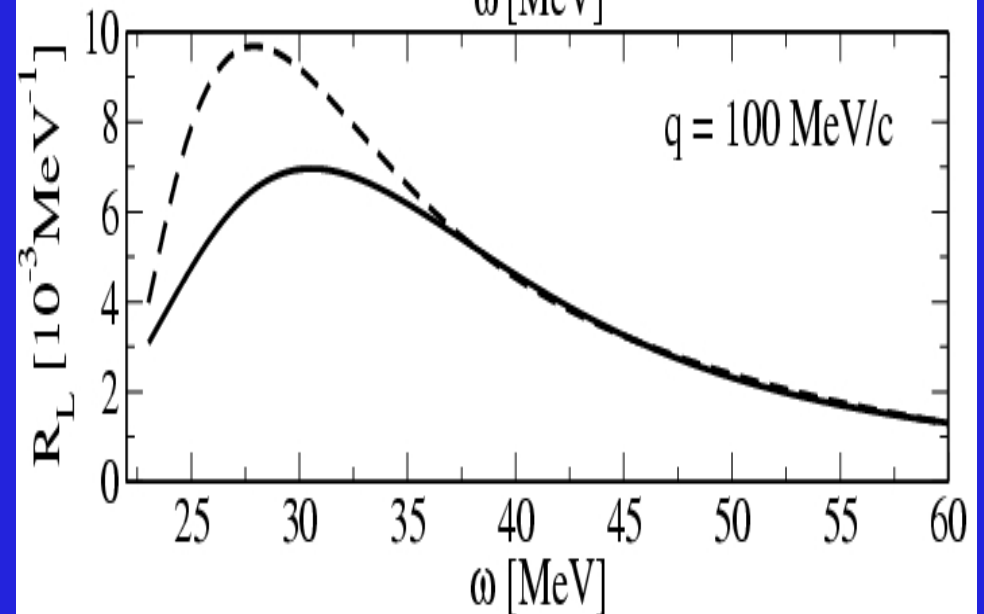
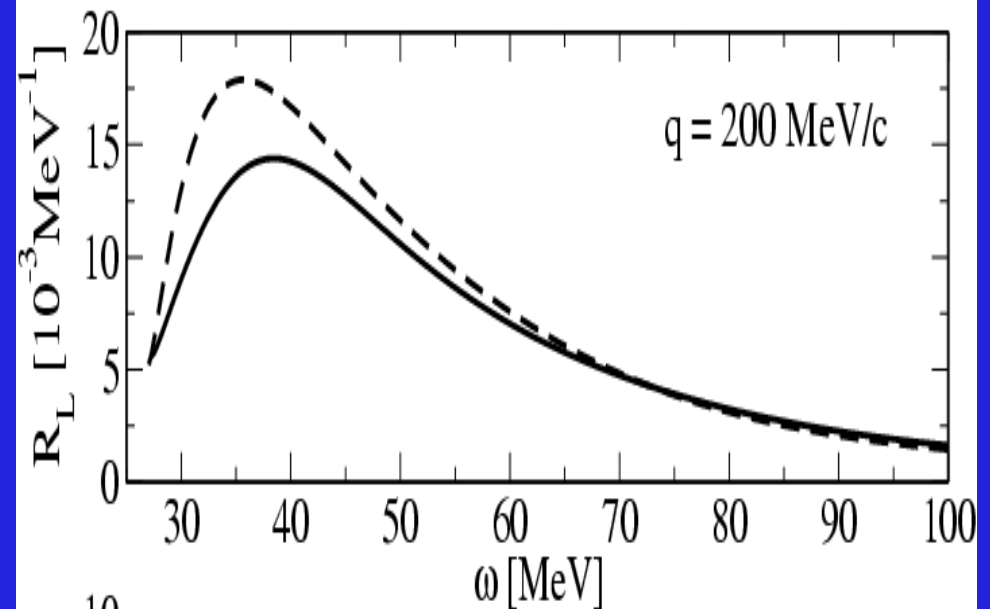


$R_L(\omega, q)$ of ${}^4\text{He}$ at lower q

----- AV18

———— AV18 +UIX

Large 3BF effects



3BF effects on peak position and peak height

	AV18	AV18+UIX	AV18	AV18+UIX	
q [MeV/c]	ω_p [MeV]	ω_p [MeV]	R_L [10^{-3}MeV^{-1}]	R_L [10^{-3}MeV^{-1}]	ΔR [%]
50	25	27	4.17	2.71	-35
100	28	30	9.70	6.90	-29
200	35	39	18.0	14.4	-20
300	54	53	13.4	12.0	-10
400	95	95	8.04	7.18	-11
500	143	147	4.82	4.35	-10

Experiments at low q would be needed!

Summary

- We have performed an *ab initio* calculation of $R_L(\omega, q)$ of ${}^4\text{He}$ with a realistic nuclear force (AV18+UIX)
- Rather strong FSI effects are found, even in peak region
- Important 3BF contribution, in particular at low q

Outlook

We are presently carrying out calculations with nuclear force AV18+TM' in order to find out if 3BF effect changes