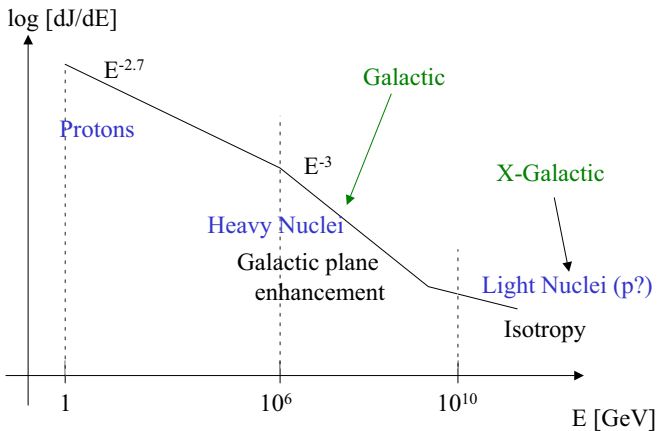


# Anisotropy of High Energy Cosmic-Rays

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In collaboration with Eli Waxmann  
arxiv:0801.4516, JCAP05(2008)006



# Isotropy of $E > 10$ EeV Cosmic Rays - Motivation

- ▶ What are the sources?

$$L_{tot} > 5 \times 10^{44} \frac{\text{erg}}{\text{s}} \left( \frac{E_p}{100 \text{ EeV}} \right)^2 \frac{\Gamma^2}{\beta}$$

(1 EeV =  $10^{18}$  eV)

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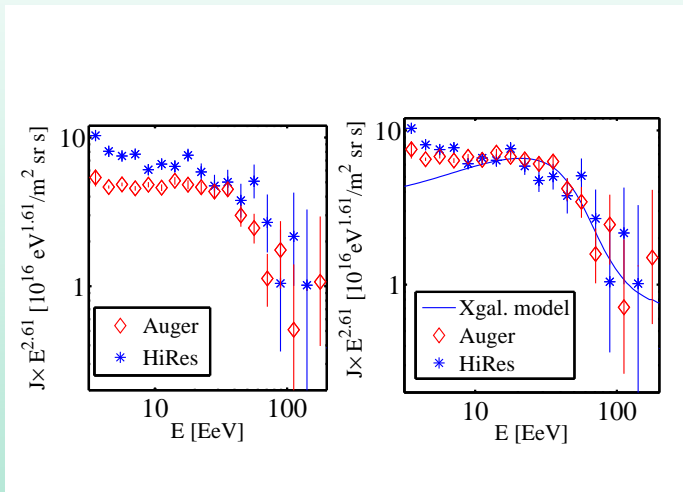
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- ▶ New Auger Observatory - 3000 km<sup>2</sup>: many events.
- ▶ Our work:

**What is the best statistics to extract the correlation between UHCRs and LLS (Large scale structures)?**

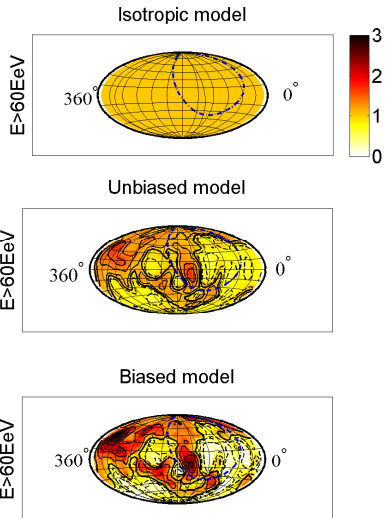
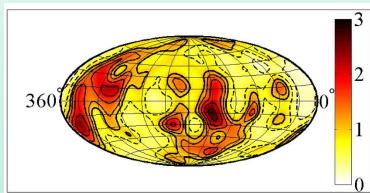
# GZK suppression

$$p\gamma \rightarrow \pi n \Rightarrow d_{GZK}(E \sim 60 \text{ EeV}) \sim 200 \text{ Mpc} \ll 4 \text{ Gpc}$$



# Cosmic ray intensity

IRAS catalog  $\rightarrow$  Integrated  
galaxy density till  
 $d = 75$  Mpc



## How to measure correlation?

- ▶ Most of the literature: Two-point angular correlation:

$$W(D) = \sum_i^N \sum_{j < i} \Theta(D - D_{ij})$$

Angular power spectrum:

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- ▶ Here: Cross Correlation ( $i$  - bin no. of  $6^\circ \times 6^\circ$ )

$$X_{C,UB} = \sum_{\{i\}} \frac{(N_i - N_{i,ISO})(N_{i,UB} - N_{i,ISO})}{N_{i,ISO}}$$

To compare:  $X_Y(\ell) = \sum_\ell \frac{(C_\ell - C_{iso,\ell})^2}{\sigma_\ell^2}$ ,  $\sigma_\ell^2$  - the variance.

## Results: cross correlation is better

$P(I/UB) \equiv$  probability for ruling out isotropy assuming unbiased.

For simulated events with Auger exposure and  $\bar{s}_0 = 10^{-4}/\text{Mpc}^3$  at 95% CL:

$E > 40 \text{ EeV}$ 100 events	P(I/UB)	P(I/B)	P(UB/B)
$X_C(\mathbf{UB})$	<b>23%</b>	<b>79%</b>	<b>42%</b>
$X_W(\{D\} = \{0 : 10 : 40\})$	7%	12%	10%
$X_C(\{\ell\} = 2)$	6%	8%	7%

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One should take the cutoff at  $E > 40$  EeV for isotropy analysis:

$X_{C,UB}$ 300 events	P(I/UB)	P(I/B)	P(UB/B)
$E > 20$ EeV (1205 events)	45%	94%	45%
<b><math>E &gt; 40</math> EeV 300 events</b>	<b>39%</b>	<b>94%</b>	<b>52%</b>
$E > 60$ EeV (94 events)	31%	87%	42%
$E > 80$ EeV (31 events)	22%	63%	24%

## Analyzing Auger's signal

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Veron-Cetty and Vernon paper:

and, with a sample of 20 and 9 cm flux densities.

This catalogue should not be used for any statistical analysis as it is not complete in any sense, except that it is, we hope, a complete survey of the literature.

HiRes: 24%.

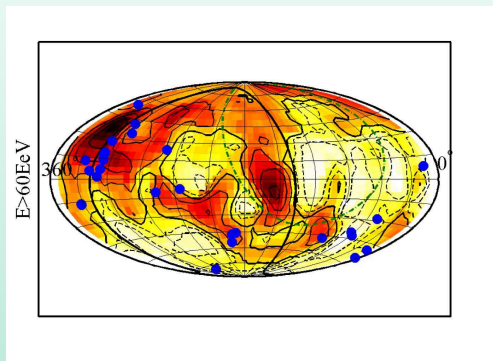
**Correlation with LSS? Unclear.**

## Analyzing Auger's signal

Auger (Science, Nov07): “inconsistency with Isotropy based on correlation with AGNs at 99% CL”.

Our cross correlation  
with LSS:

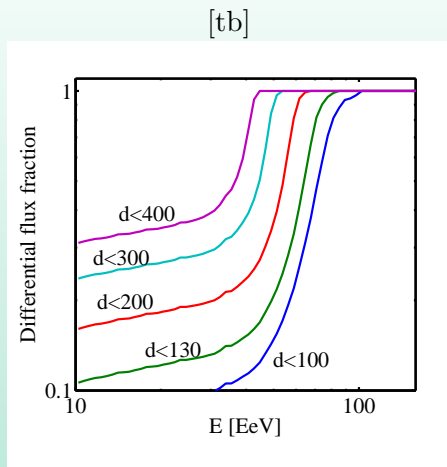
- ▶ Isotropy ruled out at 98% CL.
- ▶ Consistent with source density following LSS.



# Conclusions

1. Cross-correlation statistics is more sensitive to the expected anisotropy signature than power spectrum and two point correlation function.
2. In order to distinguish between the different bias models,  $\Delta E/E_{abs}$  should be reduced (currently  $\simeq 25\%$ ).
3. The angular distribution reported by Auger is:
  - ▶ inconsistent with Isotropy at 98% CL.
  - ▶ consistent with LSS with slight preference to a biased distribution.

# The GZK Suppression



Differential Flux function in  $\Lambda$ CDM.



# The Model

- ▶ The generation spectrum of cosmic rays above  $10^{19}$  eV:

$$\frac{d\dot{N}}{d\epsilon} = \Phi_0 \epsilon^{-\alpha} \quad \text{with } \alpha \approx 2,$$

with energy production rate of  $\Phi_0 = 0.8 \times 10^{44} \frac{\text{erg}}{\text{Mpc}^3 \text{yr}}$ .

- ▶ Proton sources trace large-scale galaxy distribution.
- ▶ The number density of CR sources is Poisson distributed.
- ▶ The protons lose energy due to interactions with CMB photons, produce  $e^+e^-$  and  $\pi$ 's ( $\Rightarrow \nu$ 's).

# The Model parameters

- ▶  $\bar{s}(z)$  - the average comoving number density of CR sources at redshift  $z$ :

$$s(z) = \bar{s}_0(1+z)^{m+3}$$

where  $\bar{s}_0 = 10^{-2} - 10^{-4}/\text{Mpc}^3$ ,  $m = 0 - 3$ .

- ▶  $b(\delta\rho)$  - a (bias) function of the local galaxy overdensity

$$\delta = \frac{\delta\rho}{\rho}$$

1. Isotropic model:  $b[\delta] = 1$
2. Unbiased model:  $b[\delta] = 1 + \delta$
3. Biased model

$$b[\delta] = \begin{cases} 1 + \delta & \delta > \delta_{\min} \\ 0 & \delta < \delta_{\min} \end{cases} .$$

## All distributions are Poisson distributions

1. The mean number density of CR sources in  $dV$  at  $z$

$$\bar{S} = \bar{s}(z)b(\delta\rho)dV$$

2. The mean number of detected CR events produced by source at redshift  $z$  is

$$\bar{N}( > E, z) = \frac{dn}{dt dA} AT = \frac{\dot{n}_0 [E_0(E, Z)] (1+z) AT}{\bar{s}_0 4\pi d_L(z)^2}$$

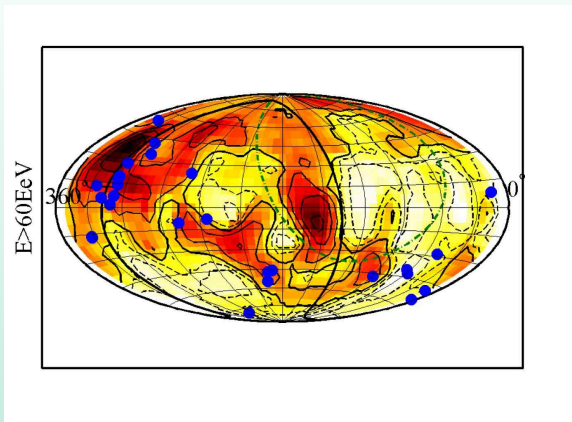
- ▶  $A$  and  $T$  are the detector area and observation time,
- ▶  $\dot{n}_0(E)$  is the CR production rate above energy  $E$  per unit volume,
- ▶  $d_L(z)$  is the luminosity distance.

3.  $\Rightarrow$  The mean number of observed CR events per steradian

$$\bar{N}_0(E, \hat{\Omega}) = \int dr r^2 \bar{N}(E, z) s(z) b[\delta\rho(z, \hat{\Omega})]$$

# Auger: correlation to AGNs?

[Auger, Science 2007]



27 events with $E > 57$ EeV	P(I)	P(UB)	P(B)
$X_{C,UB}(E > 57 \text{ EeV})$	0.9%	3.8%	20.4%
$X_{C,UB}(E > 68 \text{ EeV})$	1.5%	5.7%	27.6%

## Sensitivity to parameters

Figure: Dashed:(a)  $\alpha = -2.2$ ; (b)  $\bar{s} \propto (1+z)^0$ ;  
(c)  $\bar{s}_0 = 10^{-2} \text{Mpc}^{-3}$ ; (d) 30 EeV (50 EeV) systematic energy uncertainty (actual energy 40 EeV).

