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NGC 2300

# Cosmic Rays from Thermal Sources

**G.Wilk** (SINS, Warsaw, Poland)

and

**Z.Włodarczyk** (IF, JK Univ., Kielce, Poland)

# Cosmic rays

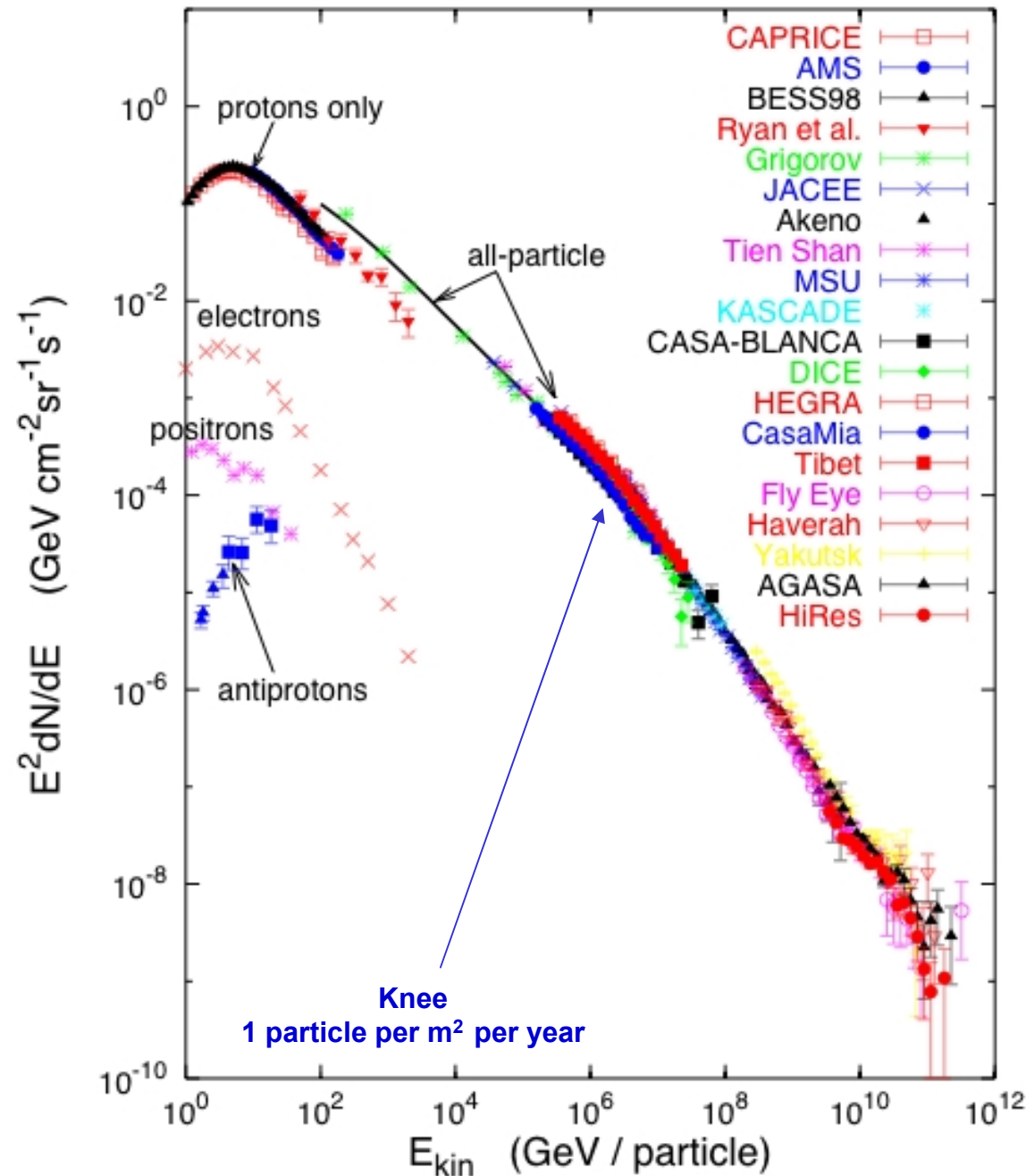
Energy spectrum spans more than **12 orders of magnitude in energy** and **24 in intensity**

- The accelerators?

Nature accelerates particles  $10^7$  times the energy of LHC!




**What are the sources?**

Energies and rates of the cosmic-ray particles



# Cosmic rays

Energies and rates of the cosmic-ray particles

CAPRICE   
AMS   
PES08 

The *knee*: different regimes of the diffusive propagation of CR ?

or: some property of the source of CR itself?

if so: what it is?

Perhaps: some change in the characteristic of the source of CR resulting in the abrupt change of distribution.

Our proposition: **it is the change in the pattern of temperature fluctuations existing in the otherwise thermal source.**  
It can be described using a generalized statistical model in which:

$$\exp(-E/T) \quad \longrightarrow \quad \exp_q(-E/T) = [1 - (1-q)E/T]^{1/(1-q)}$$

$$\text{where} \quad q = 1 + \langle (1/T)^2 \rangle / \langle (1/T) \rangle^2 = 1 + 1/C$$

is the measure of fluctuations (C is the heat capacity of the source)

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Energies and rates of the cosmic-ray particles

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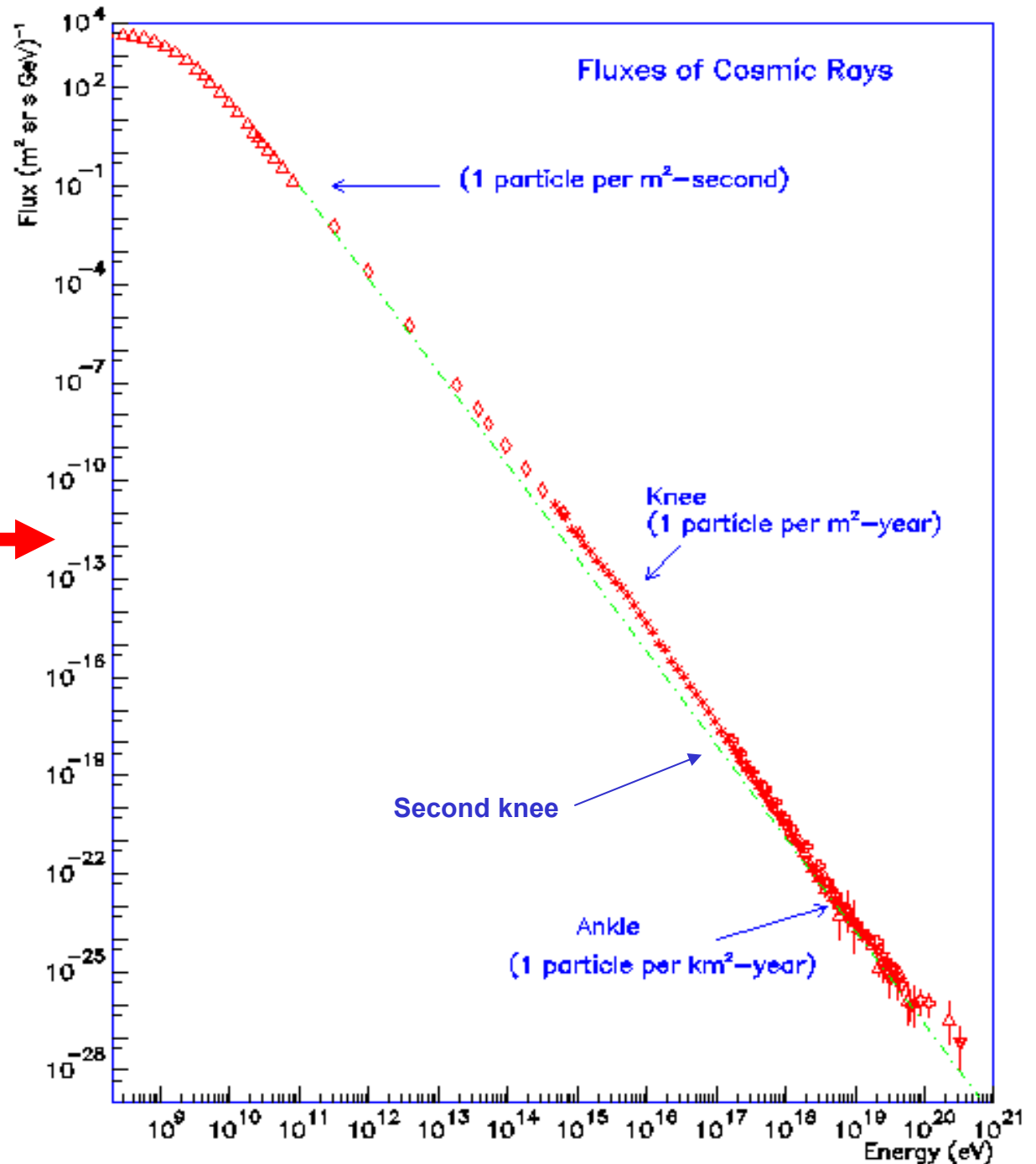
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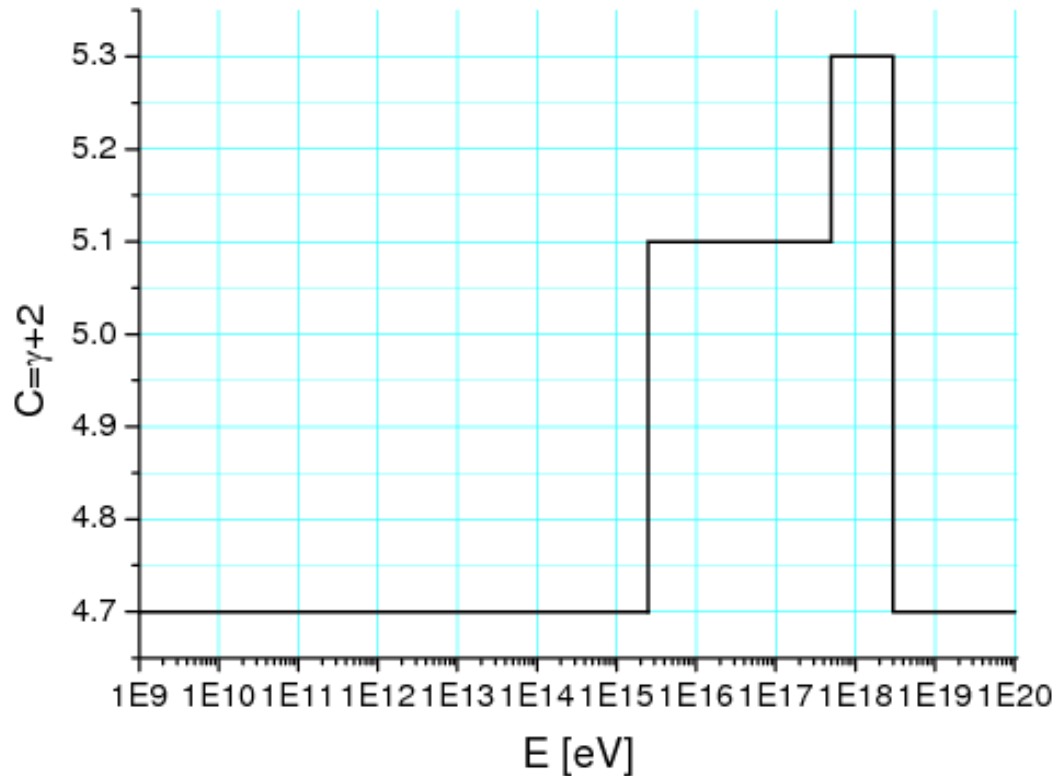
Our proposition: it is the change in the pattern of temperature fluctuations existing in the otherwise thermal source.

The temperature fluctuations in astrophysics is much discussed problem nowadays, see K.Klai et al., *Astrophys. J.* 644 (2006) 61  
and references therein

is the measure of fluctuations (C is the heat capacity of the source)

Our proposition  
is therefore  
to replace picture  
like this  
by another one  
in which the visible  
energy spectrum  
structure would be  
more visible

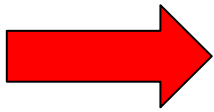




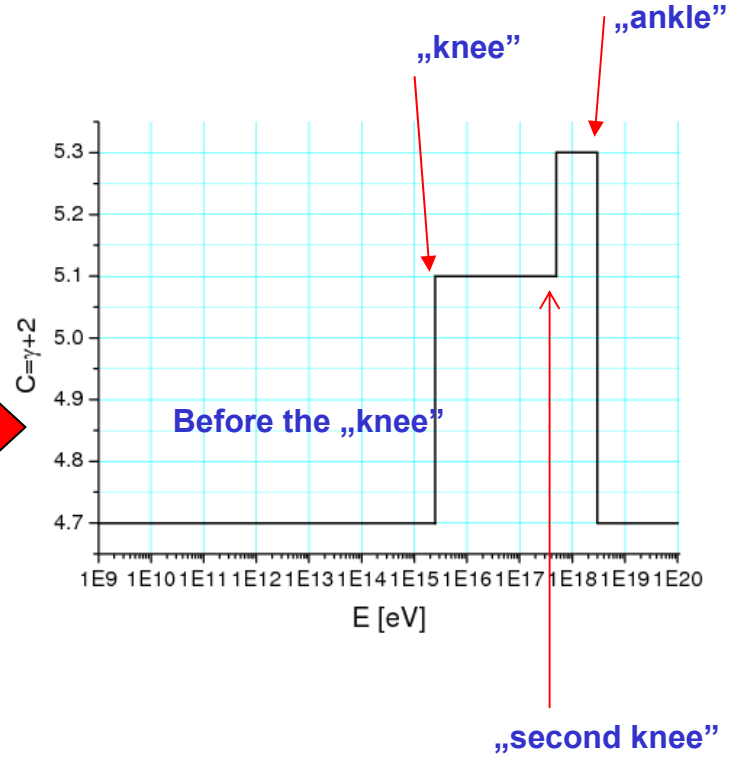
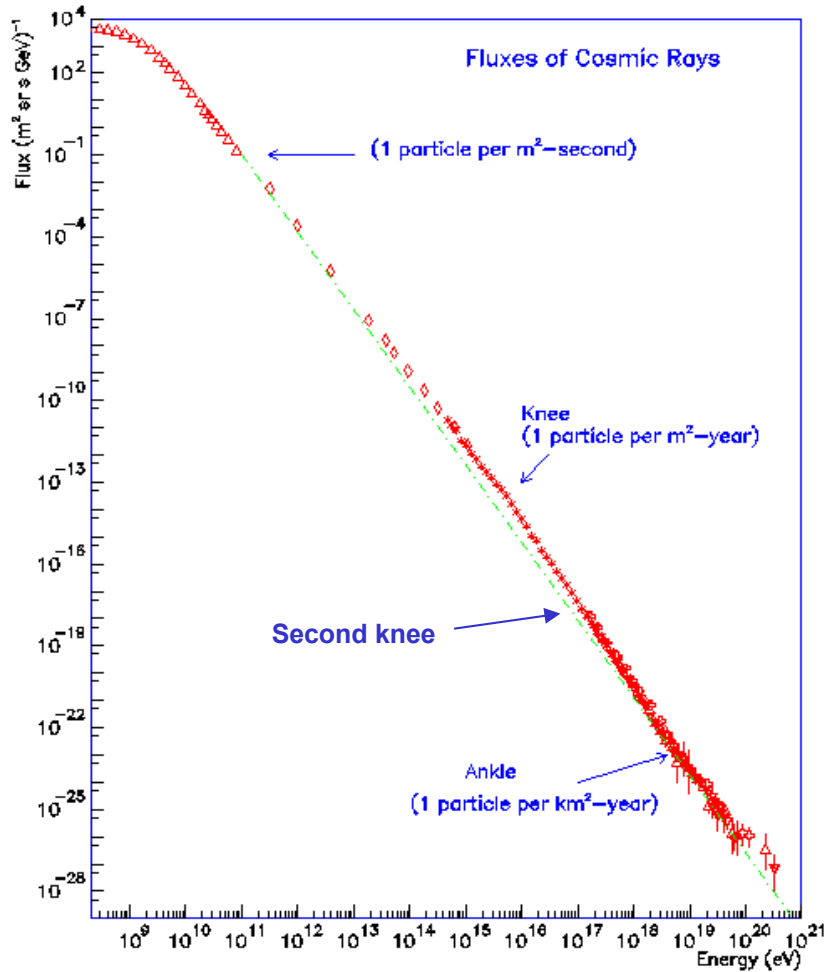
$$\Phi(E) \propto E^{-\gamma}$$

$$\gamma = \frac{3 - 2q}{q - 1}$$

Energy dependence of the heat capacity defined as,  
 **$C=1/(q-1)$ ,**  
 resulting from the measured CR energy spectrum.  
 The features of the energy spectrum of CR are now dramatically amplified forming an isolated, structured bump.



we propose to investigate such conjecture



# Energy spectrum in thermal models

$$\Phi(E) = N_0 E^2 P(E)$$

$$E \gg T$$

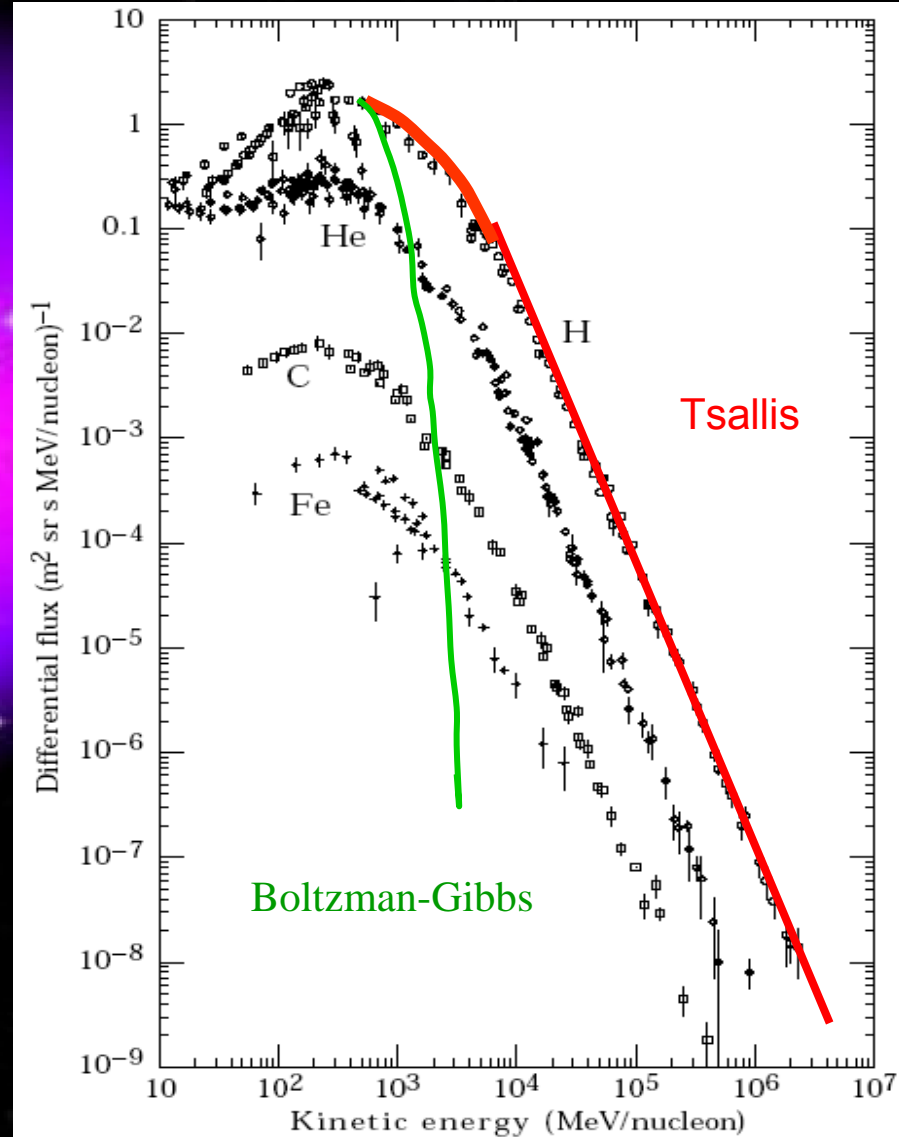
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So far we have:

(\*) C.Tsallis, J.C.Anjos, E.P.Borges, *PI A310* (2003) 372, *Fluxes of cosmic rays: a delicately balanced stationary state.*

(\*) C.Beck, *Physica A331* (2004) 173, *Generalized statistical mechanics of cosmic rays.*





C.Tsallis, J.C.Anjos, E.P.Borges, *PI A310 (2003) 372, Fluxes of cosmic rays:  
a delicately balanced stationary state.*

... We propose a phenomenological approach along the lines of nonextensive mechanics, a formalism which contains Boltzmann-Gibbs statistical mechanics as a particular case .....

... The knee then appears as a **crossover** between two fractal-like thermal regimes ... characterized by  $(T, q)$  and  $(T', q')$ .....

... Since the entropic index  $q$  is known to reflect **(multi) fractality**, the present results strongly suggest that either the generation or the transport (or both) of cosmic rays occur in the **scale invariant media** .....

**Problem:** the „temperatures” obtained are very large, of the order of 100-1000 Mev → where from could they come?

**C.Beck, Physica A331 (2004) 173, *Generalized statistical mechanics of cosmic rays.***

**.... We consider a generalized statistical mechanics model for the creation process of cosmic rays which takes into account the temperature fluctuations ....**

**...  $q=11/9$  and  $T=(5/9)T_H$  where  $T_H \approx 180$  MeV is Hagedorn temperature measured in collider experiments.....**

**This temperature seems to be overestimated because it is based on the fit to small energy region and therefore is of limited value only.**

**As before – it seems to be too large.**

(G.W, Z.W., PRL 84 (2000) 2770)

$$[1 - (1 - q)\beta_0 E]^{1/(1-q)} = \int_0^{\infty} d\beta f(\beta) \exp(-\beta E); \quad \beta = \frac{1}{T}$$

Now, if  $f(\beta)$  is such:

$$f(\beta) = \frac{1}{\Gamma(\alpha)} \left( \frac{\alpha}{\beta_0} \right)^\alpha \beta^{\alpha-1} \exp\left(-\frac{\alpha}{\beta_0} \beta\right); \quad \alpha = \frac{1}{q-1}; \quad \beta_0 = \langle \beta \rangle$$

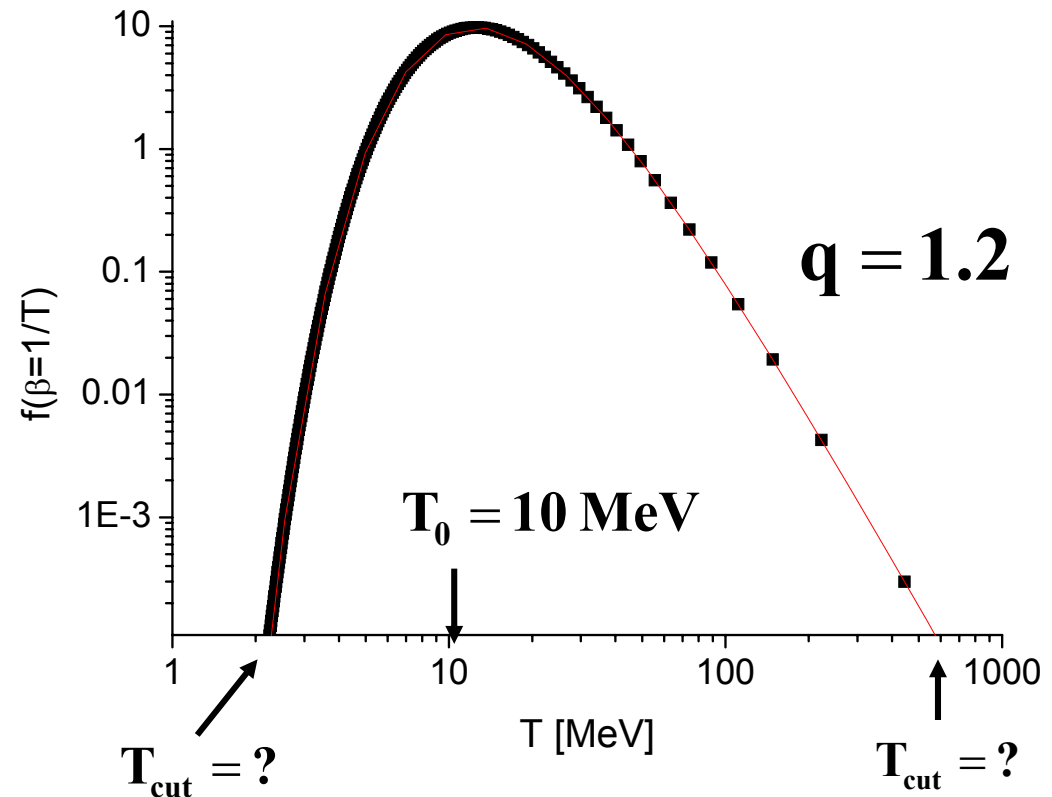
then

$$q = 1 + \frac{\langle \beta^2 \rangle - \langle \beta \rangle^2}{\langle \beta \rangle^2} = 1 + \frac{1}{C}$$

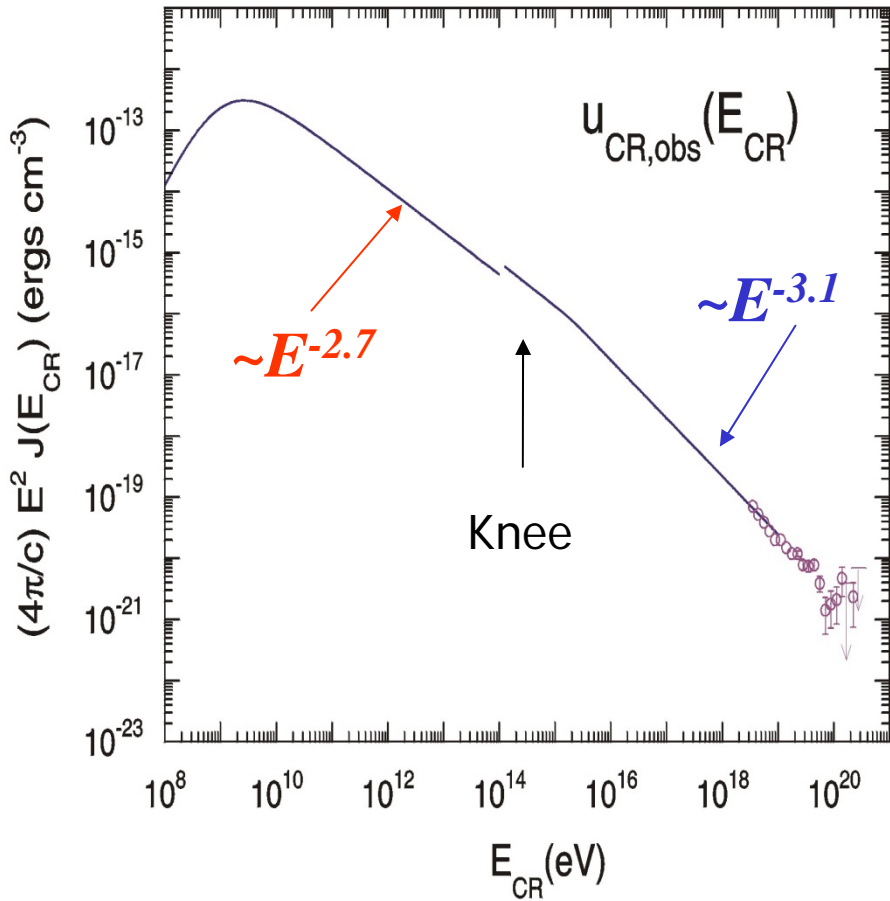
We assume now that the possible origin of such  $f(\beta)$  is temperature fluctuation in the source of CR, a possibility which is much discussed at present ( K.Klai et al., *Astrophys. J.* 644 (2006) 61 and references therein)

$$f(\beta) = \frac{1}{\Gamma(\alpha)} \left( \frac{\alpha}{\beta_0} \right)^\alpha \beta^{\alpha-1} \exp\left( -\frac{\alpha}{\beta_0} \beta \right)$$

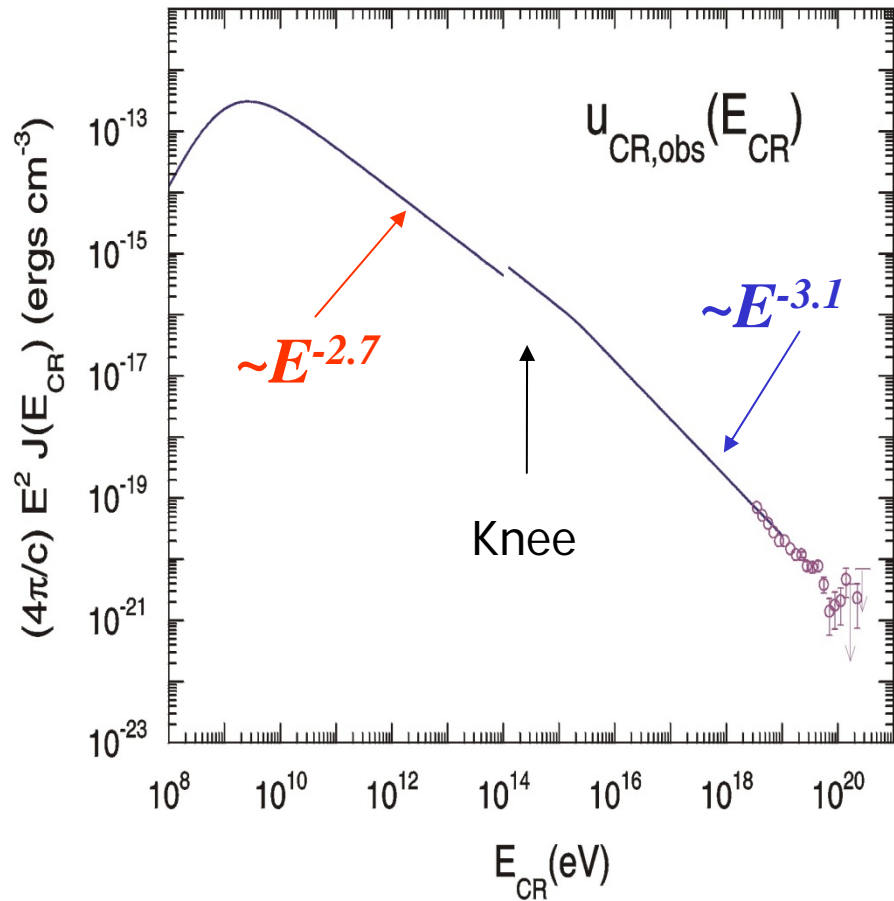
We would like to have something like this, with such small value of temperature  $T_0$



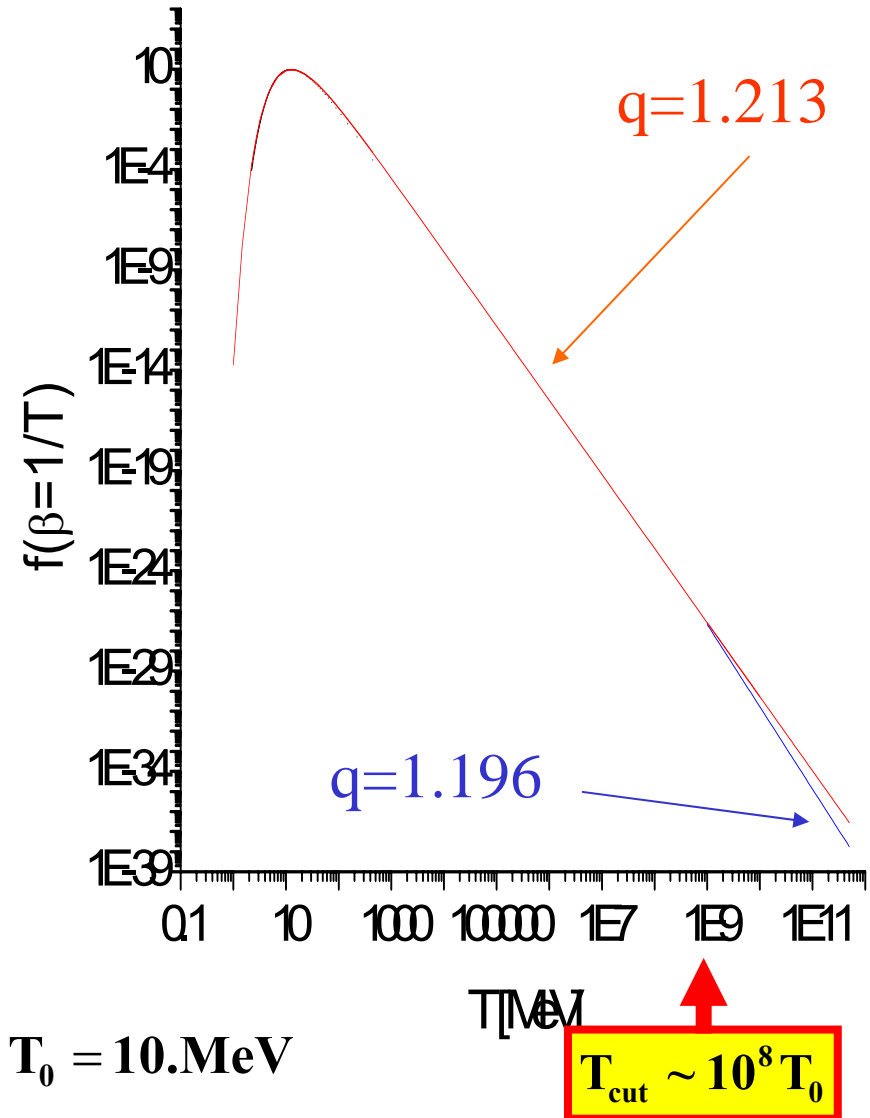
To reproduce what is observed



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one needs something like this



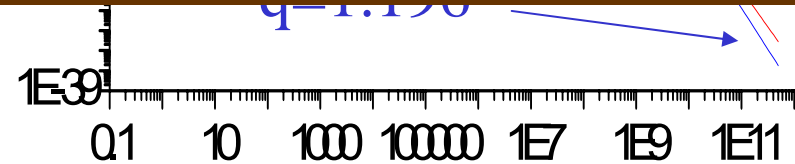
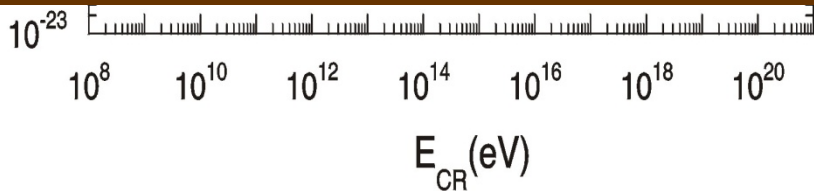
To reproduce what is observed

one needs something like this



To materialize such picture one needs a mechanism leading to the abrupt change of the entropic index  $q$  at some temperature  $T$

... possible example: **neutron star cooling...**



$T_0 = 10. \text{MeV}$

$T_{cut} \sim 10^8 T_0$

To reproduce what is observed

one needs something like this

(cf. G.Wilk and Z.Włodarczyk, arXiv:0708.1609 for details)

For example: continuous formation and breaking of Cooper pairs below

$$T=T_C \approx 0.1 - 1 \text{ MeV (or } 10^9 - 10^{10} \text{ K)}$$

This leads to the abrupt change on the heat capacities:

$$C_2/C_1 = 1.09$$

and results in  $q_1 = 1.213$  and  $q_2 = 1.196$

or in spectral indices  $\gamma_1 = 2.7$  and  $\gamma_2 = 3.1$ , as observed.

Question: but demanded change in indices is at  $T_{\text{cut}} \approx 10^{15} \text{ eV } (\approx 10^{19} \text{ K})$

Which is much too high, how this can be resolved?

At the moment we do not know ...

$(4\pi/c) E^2 J(E_{\text{CR}})$  (ergs  $\text{cm}^{-3}$ )

$10^{-13}$   
 $10^{-15}$   
 $10^{-17}$   
 $10^{-19}$   
 $10^{-21}$   
 $10^{-23}$   
10

$10^9$

.213

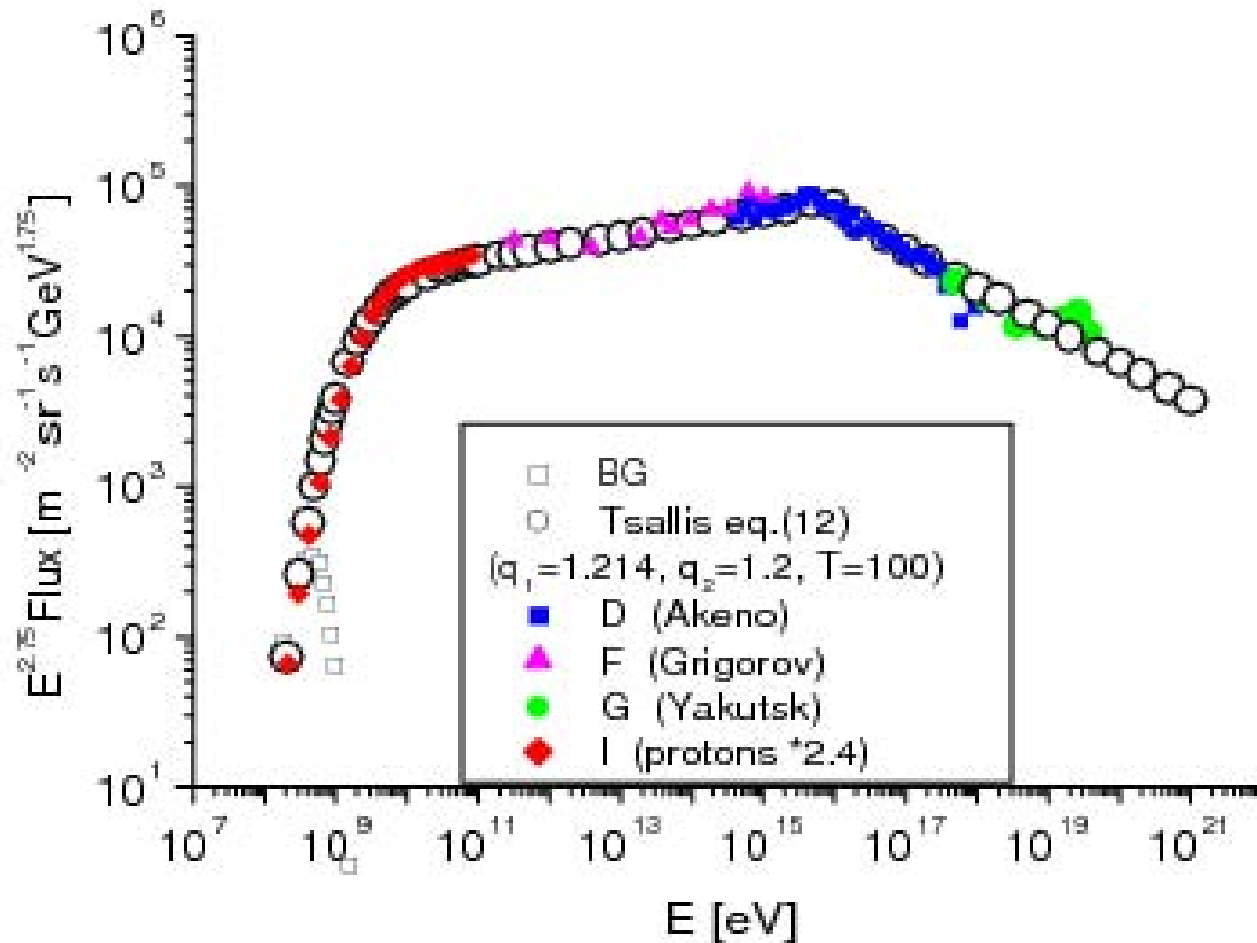
9 1E11

$$T_0 = 10 \text{ MeV}$$

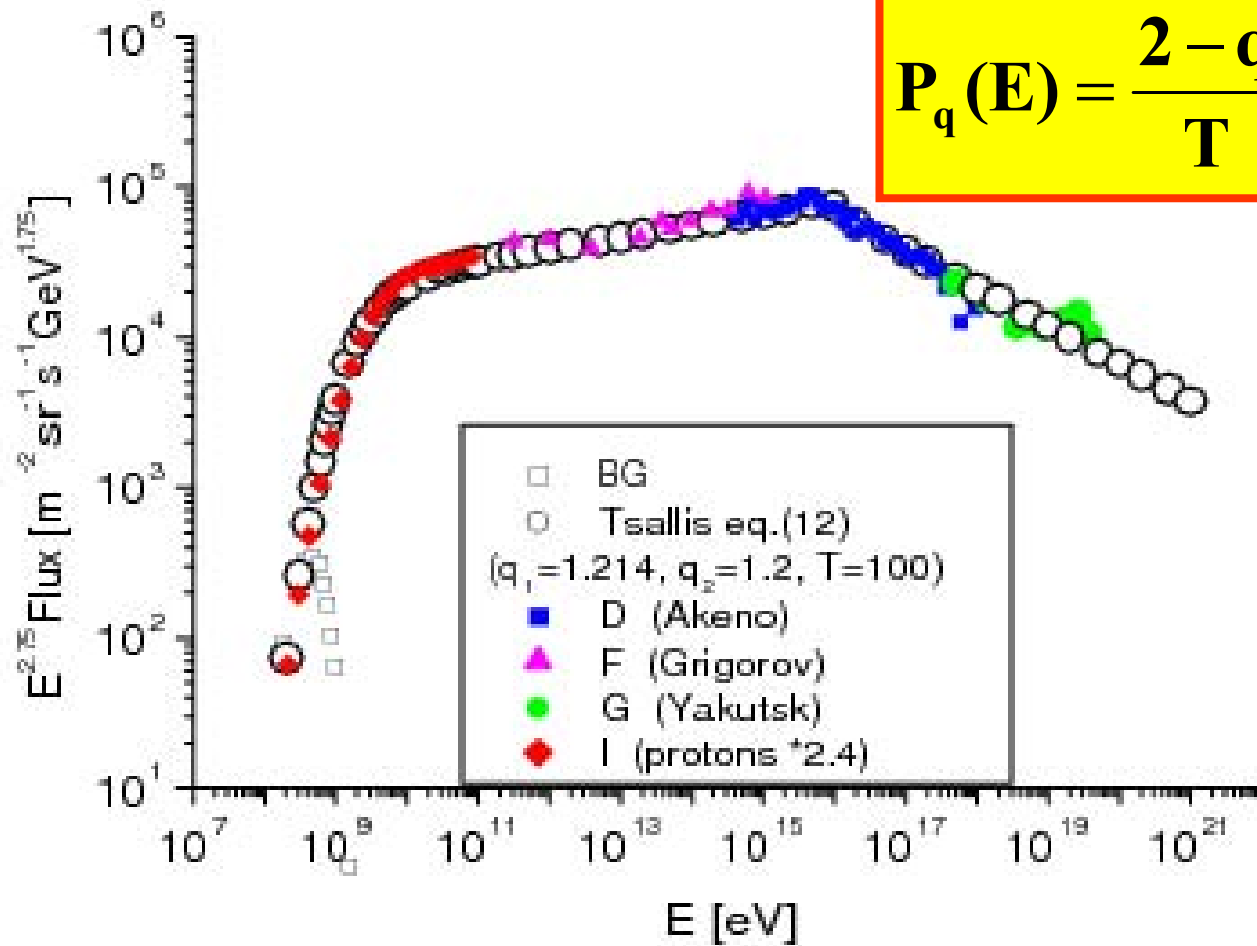
T [MeV]

$$T_{\text{cut}} \sim 10^8 T_0$$

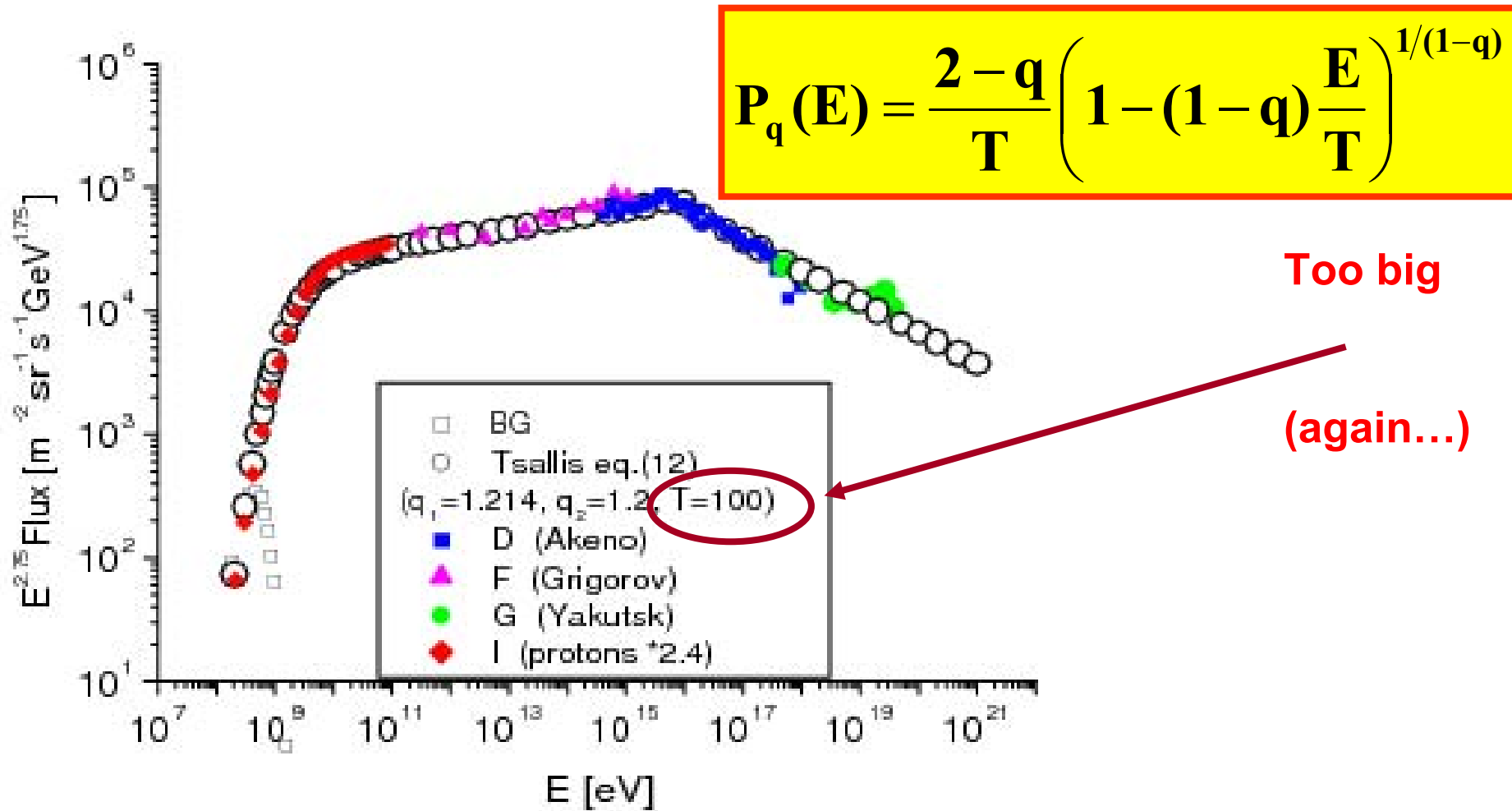




The CR energy spectrum fitted to the doubleTsallis distributions, which accounts for the whole region of energy. It was obtained assuming that fluctuations of the temperature change abruptly at some energy corresponding to  $T_{\text{cut}} \approx 10^{15} \text{ eV} \approx 10^{19} \text{ K}$ .



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$E^{2.75} \text{ Flux } [m^{-2} sr^{-1} s^{-1} GeV^{1.75}]$

**We propose the following possibility:  
keep the value of  $T \approx 100 \text{ MeV}$   
but change it meaning ....  
(but origin of that we do not know yet...)**

The  
accounts for the whole region of energy. It was obtained assuming that  
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corresponding to  $T_{\text{cut}} \approx 10^{15} \text{ eV} \approx 10^{19} \text{ K}$ .

**Proposed way out of this dilemma:**

**Add to what was proposed in our paper PRL84(2000)2770  
(which was accounting only for the possible fluctuations of T)  
also effect of the possible viscosity (\*) .**

**As a result one gets:**

- the same power-like distribution as before
- but with the previous  $T_0 = \langle T \rangle$  replaced by some effective  $T_{\text{eff}}$  :

$$T_{\text{eff}} = T_0 + (q - 1) T_{\text{visc}}$$

**where  $T_{\text{visc}}$  is some new parameter depending on the transport properties of the space through which CR propagates.**

---

(\*) G.Wilk, Z.Włodarczyk, arXiv 0810.2939[hep-ph], *Power laws in elementary and heavy-ion collisions - A story of fluctuations and nonextensivity?*

$$T_{\text{eff}} = T_0 + (q - 1) T_{\text{visc}}$$



**There are fluctuations of this  $T$  characterized by the parameter  $q$  and connected with the character of the source - for example, as discussed here ...**

$$T_{\text{eff}} = T_0 + (q - 1) T_{\text{visc}}$$



But there is also a surrounding space around the emission point, which can pump energy into some selected region from which a CR particle is emitted, it is described by the positive parameter  $T_{\text{visc}}$

→ - the total  $T_{\text{eff}}$  grows therefore with  $q$ .

$$T_{\text{eff}} = T_0 + (q - 1) T_{\text{visc}}$$

Actually, this situation is opposite to what one has in the heavy ion collisions (\*). There, in the AA collisions, one has

● region of collision in which particles are produced

and which is **hot** and

● **cold** surroundings (spectators).

Here the energy proceeds from the region of the production to the surroundings and therefore  $T$  diminishes with  $q$ .

(\*) G.Wilk, Z.Włodarczyk, arXiv 0810.2939[hep-ph], *Power laws in elementary and heavy-ion collisions - A story of fluctuations and nonextensivity?* -



To summarize this point:

(\*) In a star we have small  $T_0$  (of the order of MeV) with some fluctuations given by  $q > 1$

(\*) But if we have a flow, then in the corresponding Tsallis distribution one has  $T_{\text{eff}}$ , which can be quite large (of the order of 100 MeV)

(\*) In the spectrum of CR one observes Tsallis distribution with  $T_{\text{eff}} \sim 100$  MeV (as in the previous works by Tsallis et al.. and Beck) but now it does not mean that the temperature of the star has such a value because  $T_{\text{eff}}$  is composed from:

- the temperature of the star itself,  $T_0$ , and
- the effect of the surrounding space given by the  $T_{\text{visc}}$ .

As results now  $T_0$  can be as small as desired.

(\*) Notice: such an effect appears **ONLY** in the case of **Tsallis distribution**. For  $q \rightarrow 1$  one has  $T_{\text{eff}} \rightarrow T_0$ .



if there is no fluctuations of T one always has only  $T_0$ .

## Notice:

The temperature  $T$  which one needs seems to be of the order of MeV, i.e., of the order of the stars interior temperature. If stars are born extremaly hot in supernova explosions, with interior temperature around  $T \approx 100$  MeV, already within a day the temperature in the central region of the star will drope to something like  $0.1\text{--}10$  MeV ( $10^9\text{--}10^{10}$  K) and reach the value of 1 keV in about 100 years. The critical temperature corresponding to the nucleon superfluidity is around 1 MeV.

It means that the origing of changes of nonextensivity parameters at  $T_{\text{cut}} \approx 10^{15}$  eV  $\approx 10^{19}$  K required to fit data is still open question.

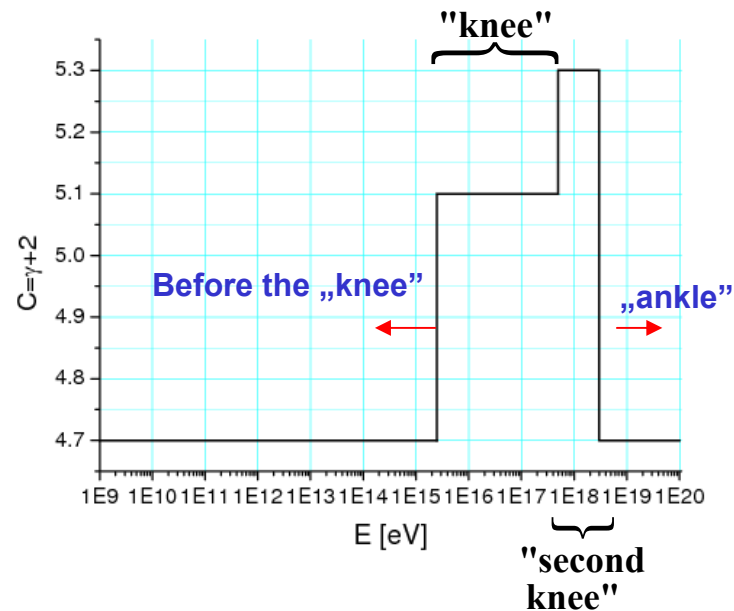
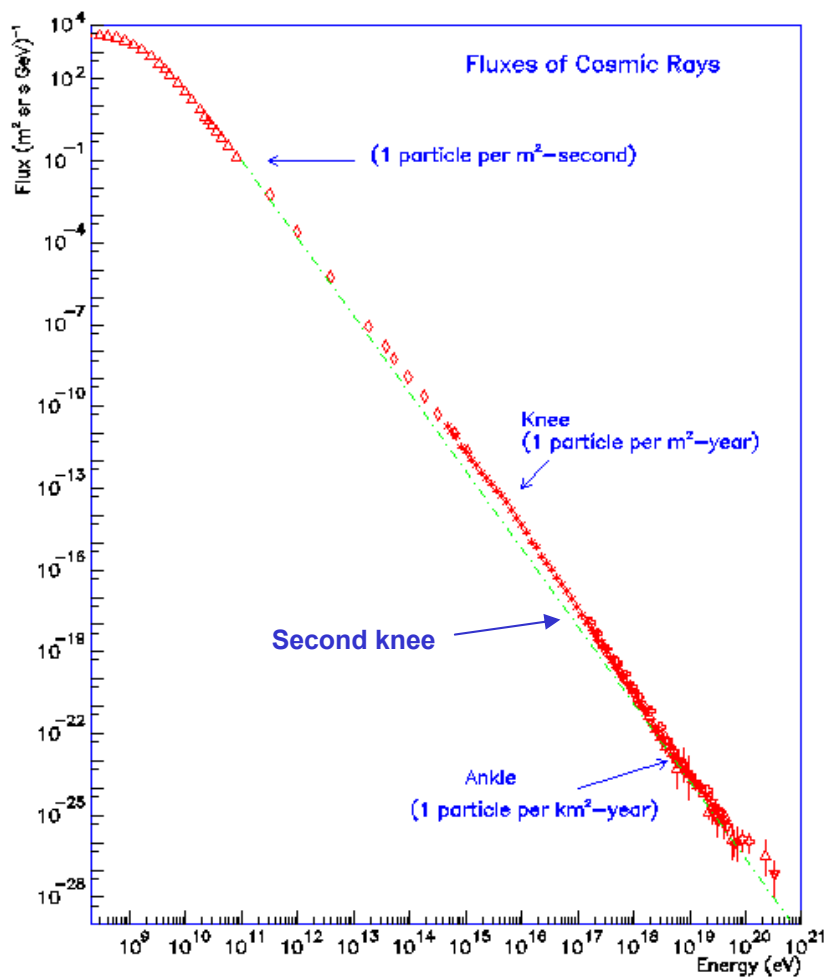
## Notice:

Perhaps this can be explained by the same mechanism which leads to large  $T_{\text{eff}}$  because, when one considers viscosity effects in stars, one observes very large abrupt changes of the viscosity coefficient which can result in effective  $T_{\text{cut}}$  of the desired order...(?)... , see, for example:

N. Andersson, *Modelling the dynamics of superfluid neutron stars*, *Astrophys Space Sci* (2007) 308: 395–402

It means that the origing of changes of nonextensivity parameters at  $T_{\text{cut}} \approx 10^{15} \text{ eV} \approx 10^{19} \text{ K}$  required to fit data is still open question.

# To summarize: we propose to investigate such idea



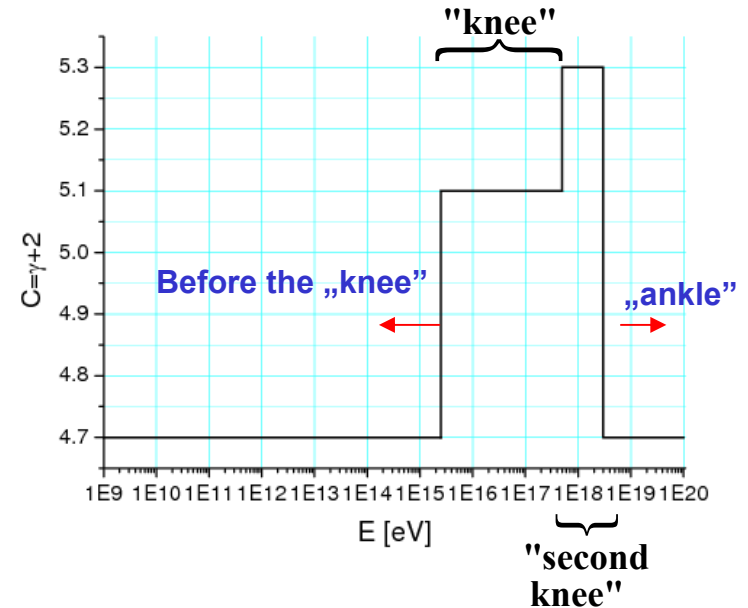
## To summarize: we propose to investigate such idea

Use nonextensive thermal approach in which parameter  $q$  is connected with the heat capacity  $C=1/(q-1)$

$C$  acts as a kind of magnifying glass converting all subtleties of the shape of the energy flux of CR into a much more pronounced and structured bump.

Its importance would parallel long-standing discussion of the origin of the knee-like structure of the CR energy spectrum, but exposed in much more dramatic and visible way.

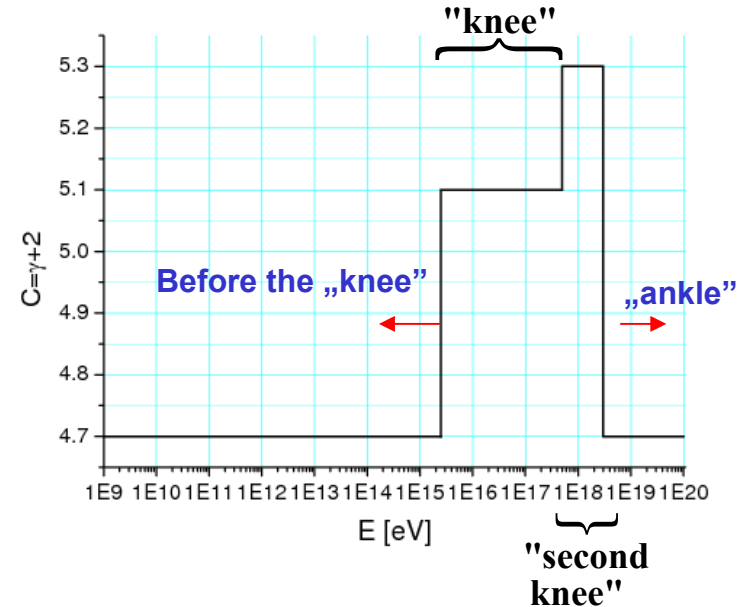
At the moment we can only offer two examples of the possible explanation of this feature.



## Examples of the possible explanation of this feature: (I)

(I) This effect is due to the change of the effective number of degrees of freedom in the incoming projectiles with energy.

Assuming that most of CR consist of protons, which are build from three quarks, one could speculate that consecutive bumps correspond to excitations from single proton to proton plus one quark and two quark structure, after exciting all three quarks one comes back to the original situation (\*).

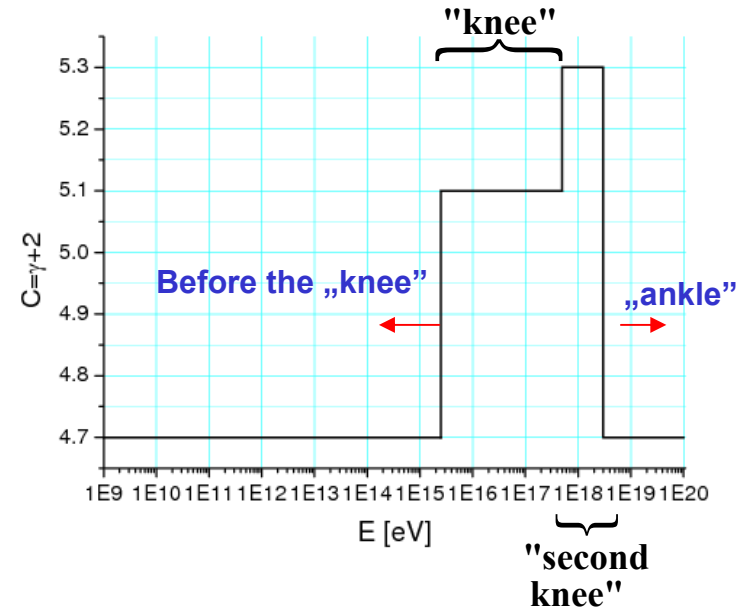


(\*) Much in the spirit of the changes observed when ice becomes water and this becomes steam – there the corresponding  $C$ 's also show characteristic jump, see P.Fraundorf, *Am.J.Phys.* **71** (2003) 1142.

## Examples of the possible explanation of this feature: (II)

(II) This effect reflects the behavior of heat capacity in Fermi liquids.

O.V.Maxwell, *Astrophys. J.* 231 (1979) 201.



## Examples of the possible explanation of this feature: (II)

### (II) This effect reflects the behavior of the heat capacity in Fermi liquids (\*).

The proton's heat capacity is proportional to the ratio of the effective mass of the proton in the neutron fluid to the mass of the free proton:  $C \sim m^*/m$

In the case of a mixture of Fermi liquids the proton effective mass  $m^*$  is affected by the interactions with neutrons and other protons and is given by

$$\frac{m^*}{m} = 1 + \frac{1}{3} D_p \left[ f_1^{pp} + \left( \frac{k_{F_n}}{k_{F_p}} \right)^2 f_1^{pn} \right]$$

where  $D_p$  denotes the density of quasiparticle states at Fermi surface given by the wave vectors  $k_{F_n}$  and  $k_{F_p}$  for the, respectively, neutrons and protons whereas  $f_1^{pp}$  and  $f_1^{pn}$  are Landau parameters (\*\*).

(\*) O.V.Maxwell, *Astrophys. J.* 231 (1979) 201.

(\*\*) M.Borumand, R.Joynt and W.Kluźniak, *Phys. Rev. C* 54 (1996) 2745.



## Examples of the possible explanation of this feature: (II)

(II) This effect reflects the behavior of heat capacity in Fermi liquids (\*).

We start with the superfluid liquid with (here  $m^*$  represents the effective mass for the  $pp$  and  $pn$  interactions),

$$C_1 = 4.7$$

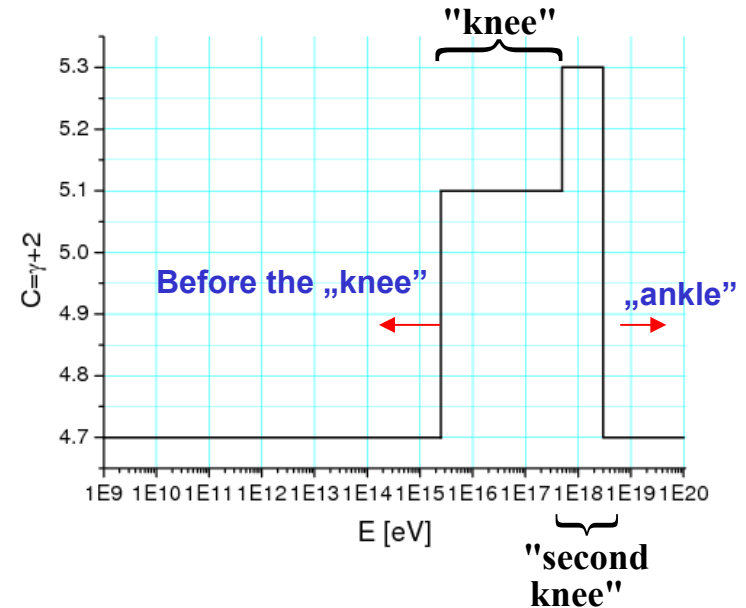
When energy increases we stop to see nuclear interactions and (with  $m^*$  representing  $pp$  interactions only).

$$C_2 = 5.1$$

Finally, for larger  $T$ , we have Fermi gas with

$$C_3 = 5.3$$

and, still further, we return again to the usual Fermi liquid .



(\*) O.V.Maxwell, *Astrophys. J.* 231 (1979) 201.

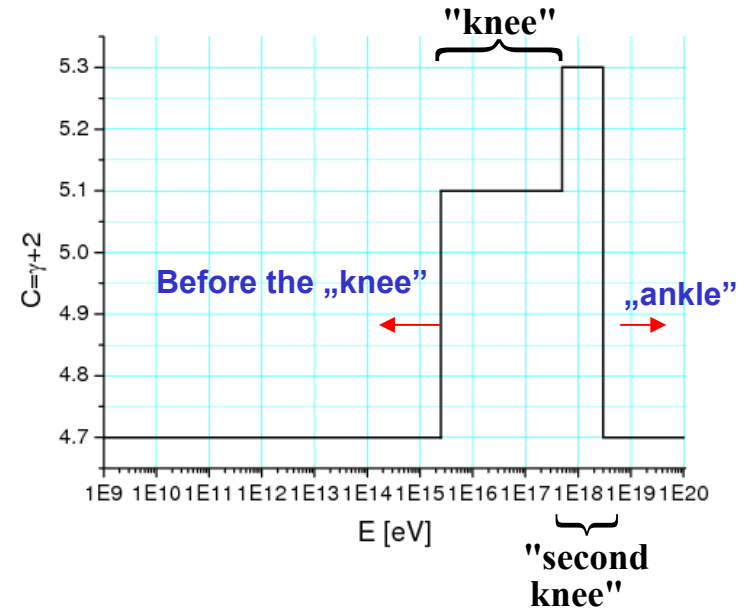
## Examples of the possible explanation of this feature: (II)

(II) This effect reflects the behavior of heat capacity in Fermi liquids (\*).

It is worth to remember that fluctuations of temperature we are talking about here refer to fluctuations in the small region  $V$ .

For Fermi liquid the heat capacity expressed in units of Boltzmann constant  $k_B$  (i.e., for  $k_B = 1$ ) is of the order  $C \approx 3 \cdot 10^{35} \text{ cm}^{-3}$  (\*\*).

Therefore, taking values of  $C$  estimated from the slope of the primary CR spectra one gets that the size of the region of fluctuations is  $V \sim 10^4 \text{ fm}^3$ .



(\*) O.V.Maxwell, *Astrophys. J.* 231 (1979) 201.

(\*\*) D.G.Yakovlev and V.A.Urpin, *Sov. Astron. Lett.* 7 (2) (1981) 88.

# Summary

- Nonextensive statistics successfully describes the smooth power-like spectrum

- We propose to place the origin of the proposed temperature fluctuations in a source of CR (rather than in the temperature distribution of CR sources). Actually, one needs a composed pattern of fluctuations with an abrupt change in the  $q$ -parameter at  $T \sim \text{PeV}$  in order to reproduce region of "knee"; its origin remains at the moment unknown...

- The observed temperatures  $\langle T \rangle$  seem to be of the order of  $\sim \text{MeV}$  (i.e., of the order of the  $T$  in the interior of stars), which is much smaller than values obtained by Tsallis and al., and by Beck.

- To get  $\langle T \rangle \sim 100 \text{ MeV}$  (as required by data on the CR spectra) one has to allow for the action of the surroundings of the source resulting in  $T_{\text{eff}}$  of that order.

*The*

*End*